

# Foundations of Energy Harvesting and Energy Cooperating Wireless Communications



**PennState**

Wireless Communications  
& Networking Laboratory  
**WCAN@PSU**

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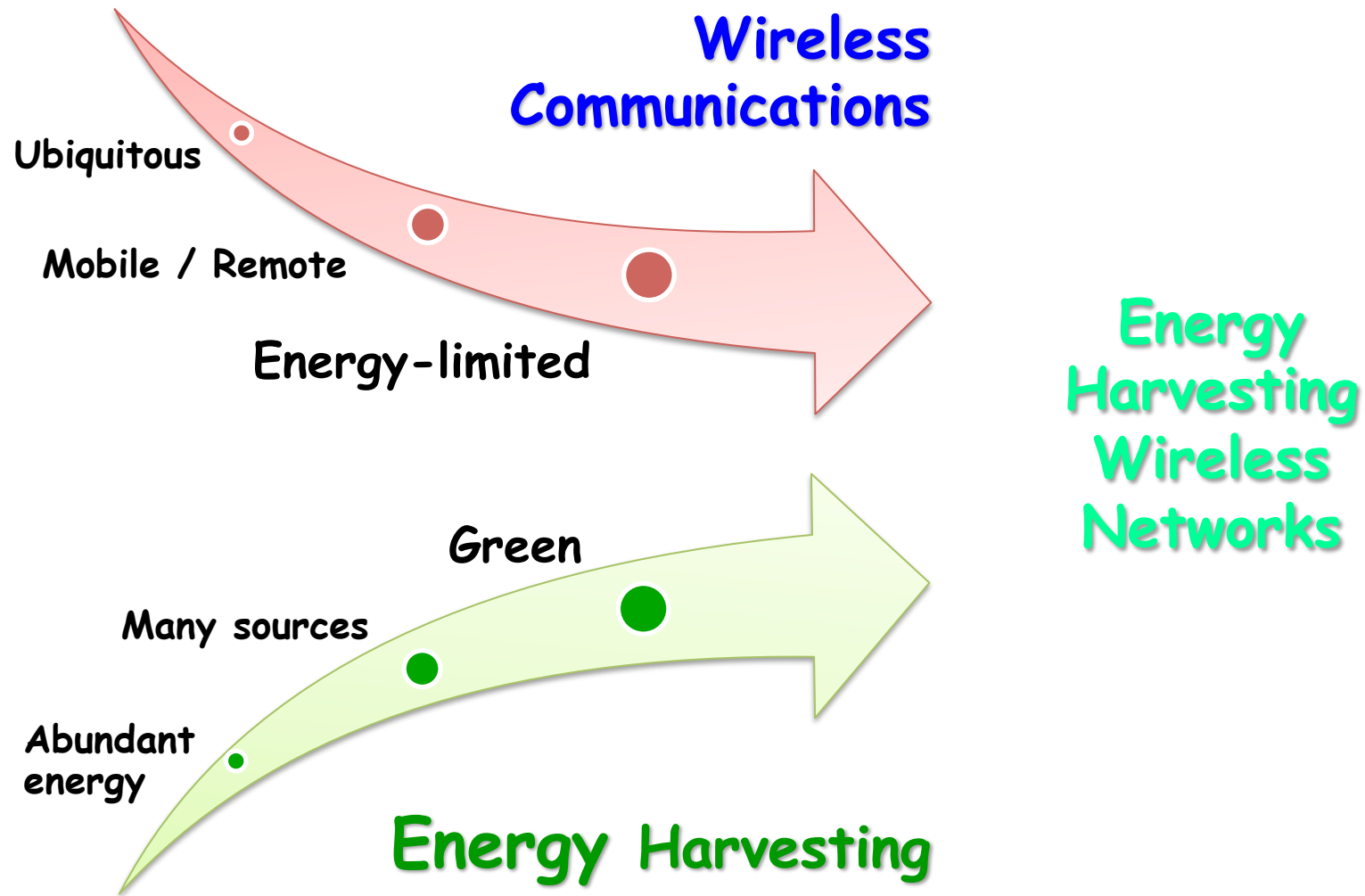
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# Introduction

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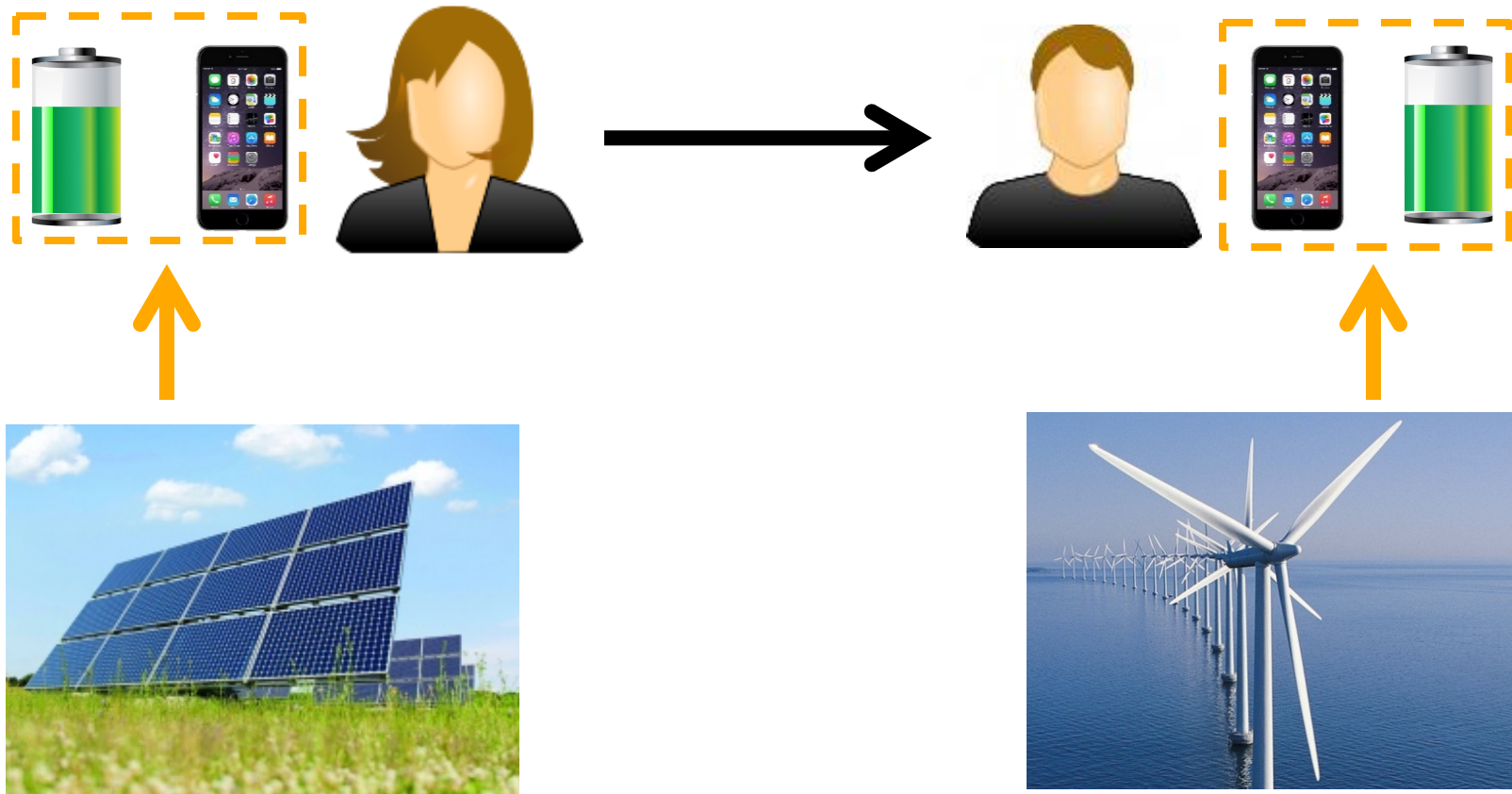


# Energy Harvesting Networks

- Wireless networking with rechargeable (energy harvesting) nodes:
  - Green, self-sufficient nodes,
  - Extended network lifetime,
  - Smaller nodes with smaller batteries.

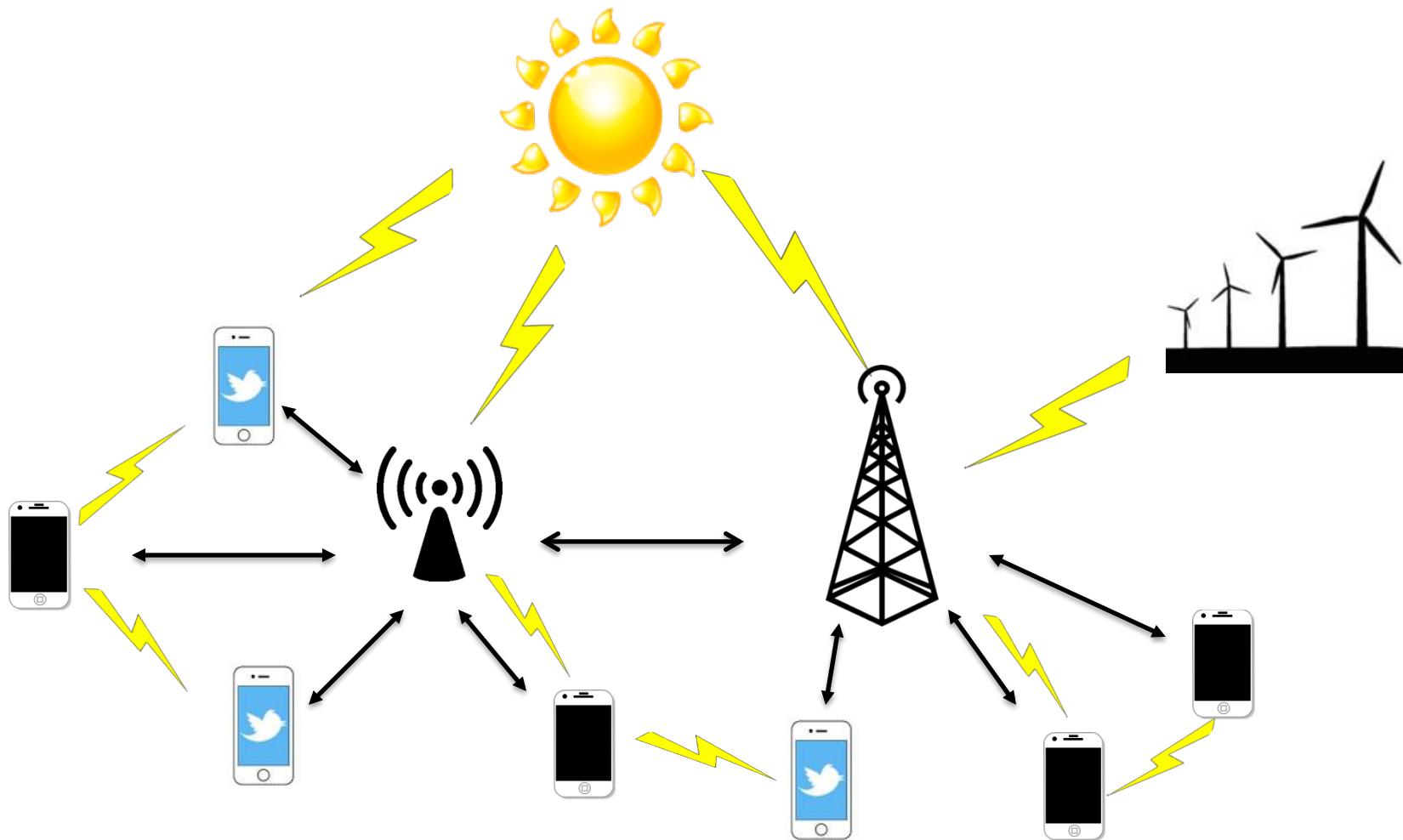


# What could EH bring to communications?





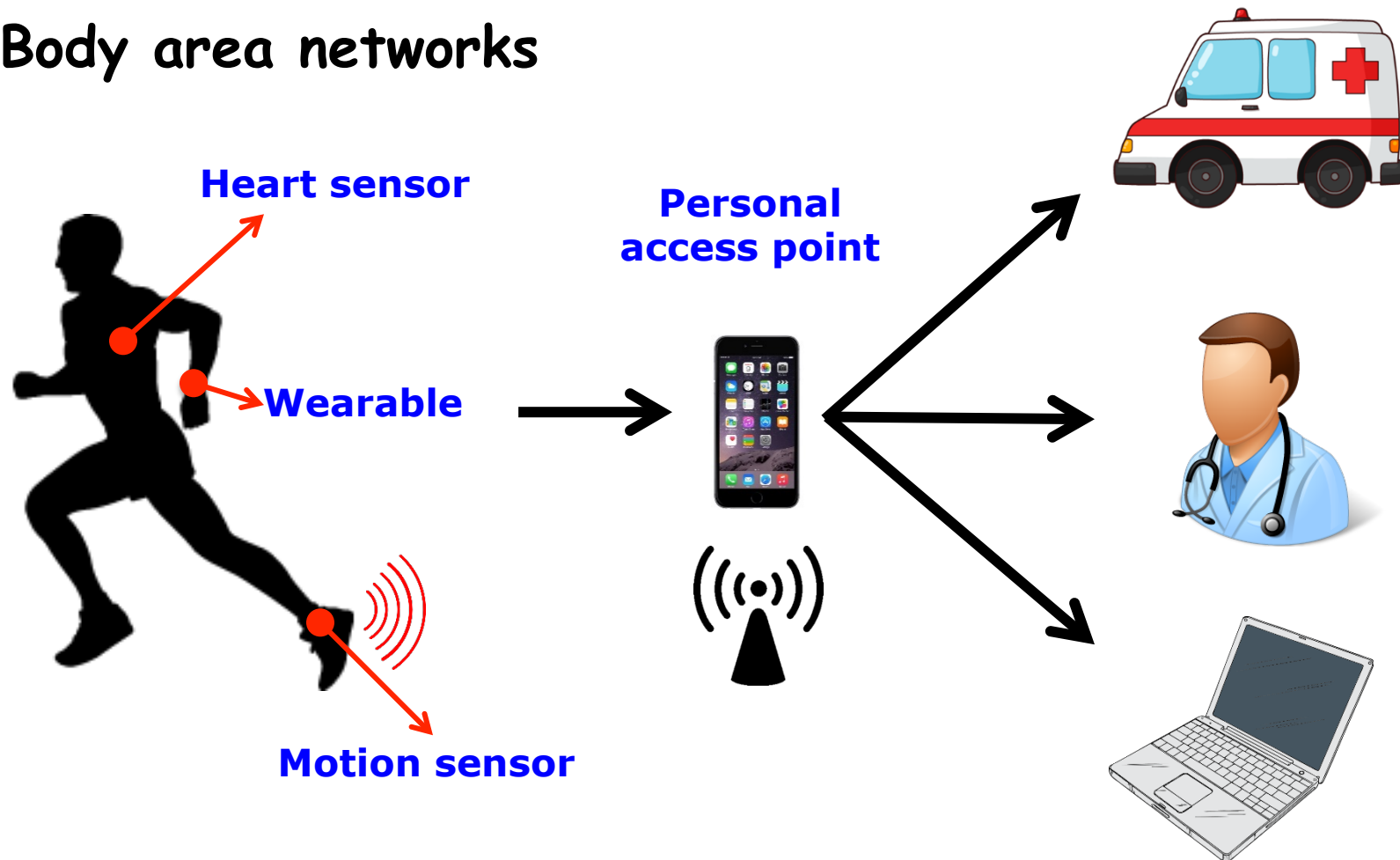
# Wireless Energy Cooperation





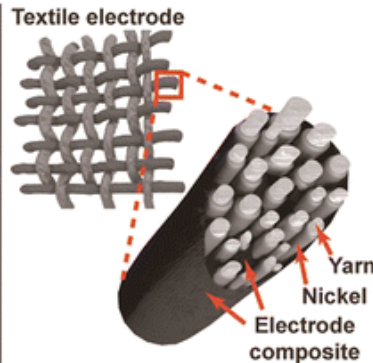
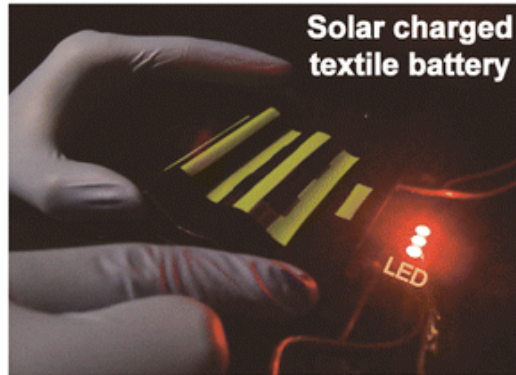
# Energy Harvesting Applications

## Body area networks



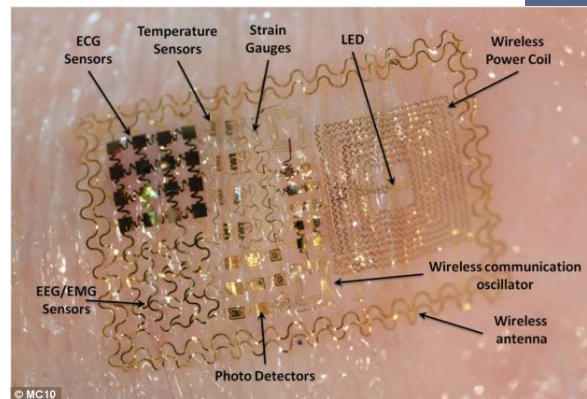


# Energy Harvesting Applications



KAIST's Solar charged  
textile battery

MC10's biostamps  
for medical monitoring,  
powered **wirelessly**



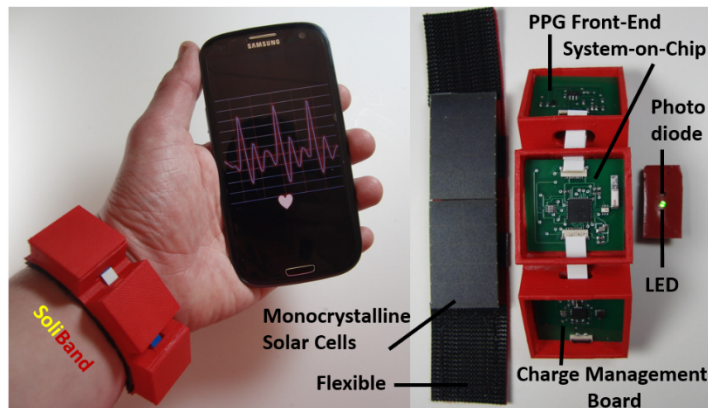
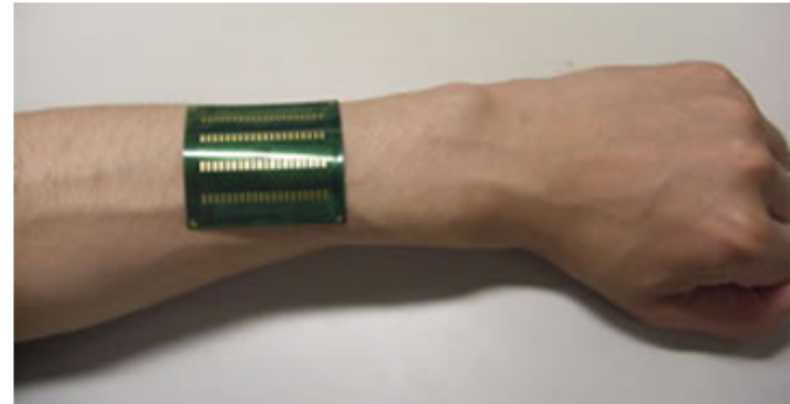
**Image Credits:** (top) <http://pubs.acs.org/doi/abs/10.1021/nl403860k#aff1> (bottom) ) <http://www.dailymail.co.uk/sciencetech/article-2333203/Moto-X-Motorola-reveals-plans-ink-pills-replace-ALL-passwords.html>





# Energy Harvesting Applications

Fujitsu's hybrid device  
utilizing heat or light.



Health tracker utilizing solar  
cells

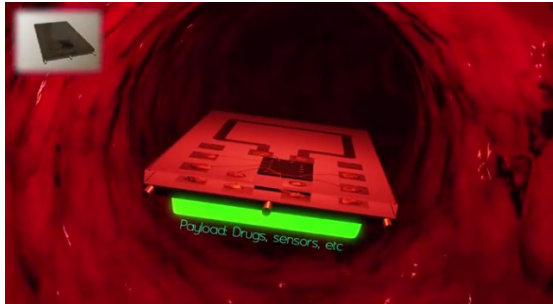


**Image Credits:** (top) <http://www.fujitsu.com/global/news/pr/archives/month/2010/20101209-01.html>  
(bottom) <https://assist.ncsu.edu/research/>

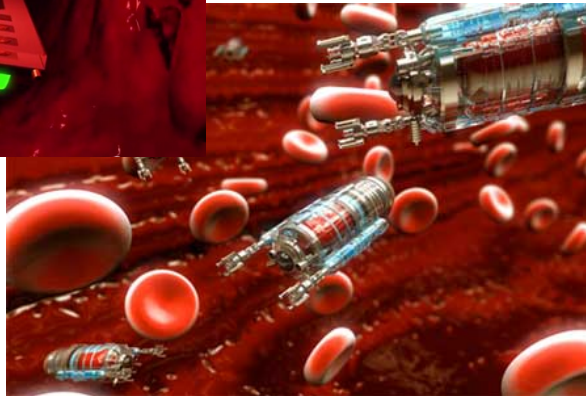




# Energy Harvesting Applications



In-body (intravascular) wireless devices



Proteus Biomedical pills,  
powered by **stomach acids**



**Image Credits:** (top) <http://www.extremetech.com/extreme/119477-stanford-creates-wireless-implantable-innerspace-medical-device>  
(middle) <http://www.imedicalapps.com/2012/03/robotic-medical-devices-controlled-wireless-technology-nanotechnology/>  
(bottom) <http://scitechdaily.com/smart-pills-will-track-patients-from-the-inside-out/>



# What is in it for us?

- New: communication theory of EH nodes
- New: information theory of EH nodes

Key new ingredient:

A **set of energy feasibility constraints** based on harvests govern the communication resources.



# Communications

- **New Wireless Network Design Challenge:**  
A **set of energy feasibility constraints** based on harvests govern the communication resources.
- **Design question:**  
When and at what rate/power should a "rechargeable" (energy harvesting) node transmit?
- **Optimality? Throughput; Delivery Delay**
- **Outcome: Optimal Transmission Schedules**



# Two main metrics

- **Short-Term Throughput Maximization (STTM):**

Given a deadline, maximize the number of bits sent before the end of transmission.

- **Transmission Completion Time Minimization (TCTM):**

Given a number of bits to send, minimize the time at which all bits have departed the transmitter.



# ST Throughput Maximization

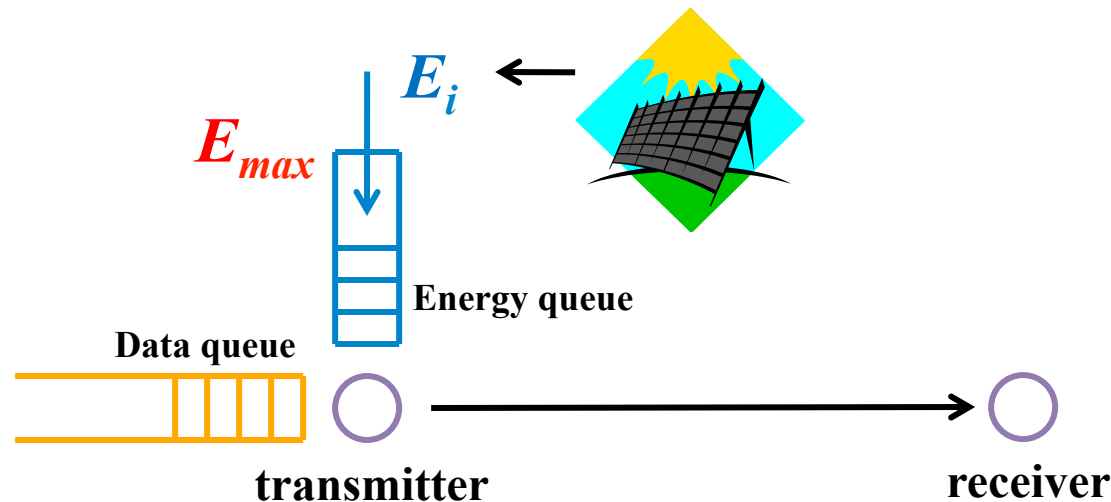
[Tutuncuoglu-Y. 2012]

- One Energy harvesting transmitter.
- Find optimal power allocation/transmission policy that departs maximum number of bits in a given duration  $T$ .
- Energy available intermittently.
- Up to a certain amount of energy can be stored by the transmitter → BATTERY CAPACITY.



# System Model

- Energy harvesting transmitter:

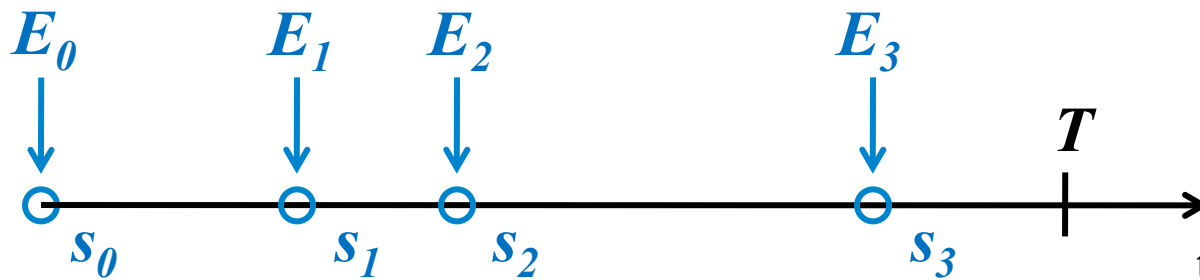


- Transmitter has **data** to send by deadline  $T$
- Energy **arrives intermittently** from harvester
- Stored in a **finite battery** of capacity  $E_{max}$



# System Model

- Energy arrivals of energy  $E_i$  at times  $s_i$



- Arrivals known **non-causally** by transmitter,
- Design parameter: **power**  $\rightarrow$  **rate**  $r(p)$ .



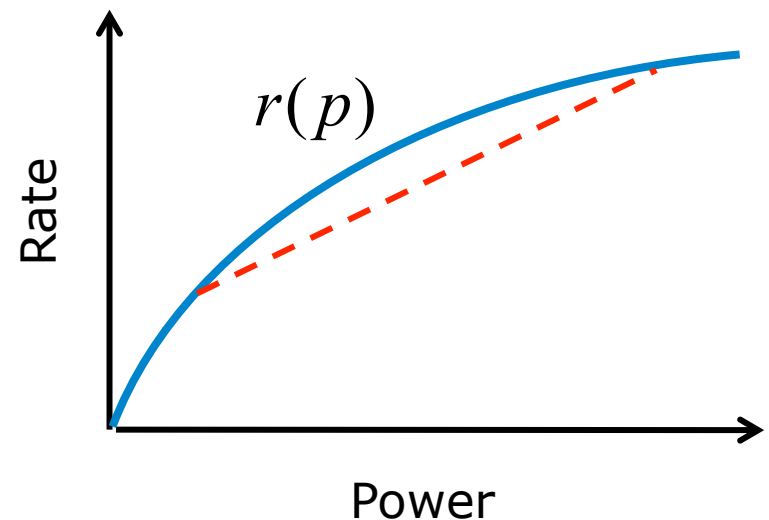


# Power-Rate Function

- Transmission with power  $p$  yields a rate of  $r(p)$

- Assumptions on  $r(p)$ :

- i.*  $r(0)=0$ ,  $r(p) \rightarrow \infty$  as  $p \rightarrow \infty$
- ii.* increases monotonically in  $p$
- iii.* strictly concave
- iv.*  $r(p)$  continuously differentiable



Example: AWGN Channel, 
$$r(p) = \frac{1}{2} \log \left( 1 + \frac{p}{N} \right)$$



# Notations and Assumptions

- Power allocation function:  $p(t)$
- Energy consumed:  $\int_0^T p(t)dt$
- Short-term throughput:  $\int_0^T r(p(t))dt$

Concave rate in power  $\rightarrow$  Given a fixed energy, a longer transmission with lower power departs more bits.



# Energy Constraints

(Energy arrivals of  $E_i$  at times  $s_i$ )

- **Energy Causality:**  $\sum_{i=0}^{n-1} E_i - \int_0^{t'} p(t) dt \geq 0 \quad s_{n-1} \leq t' \leq s_n$

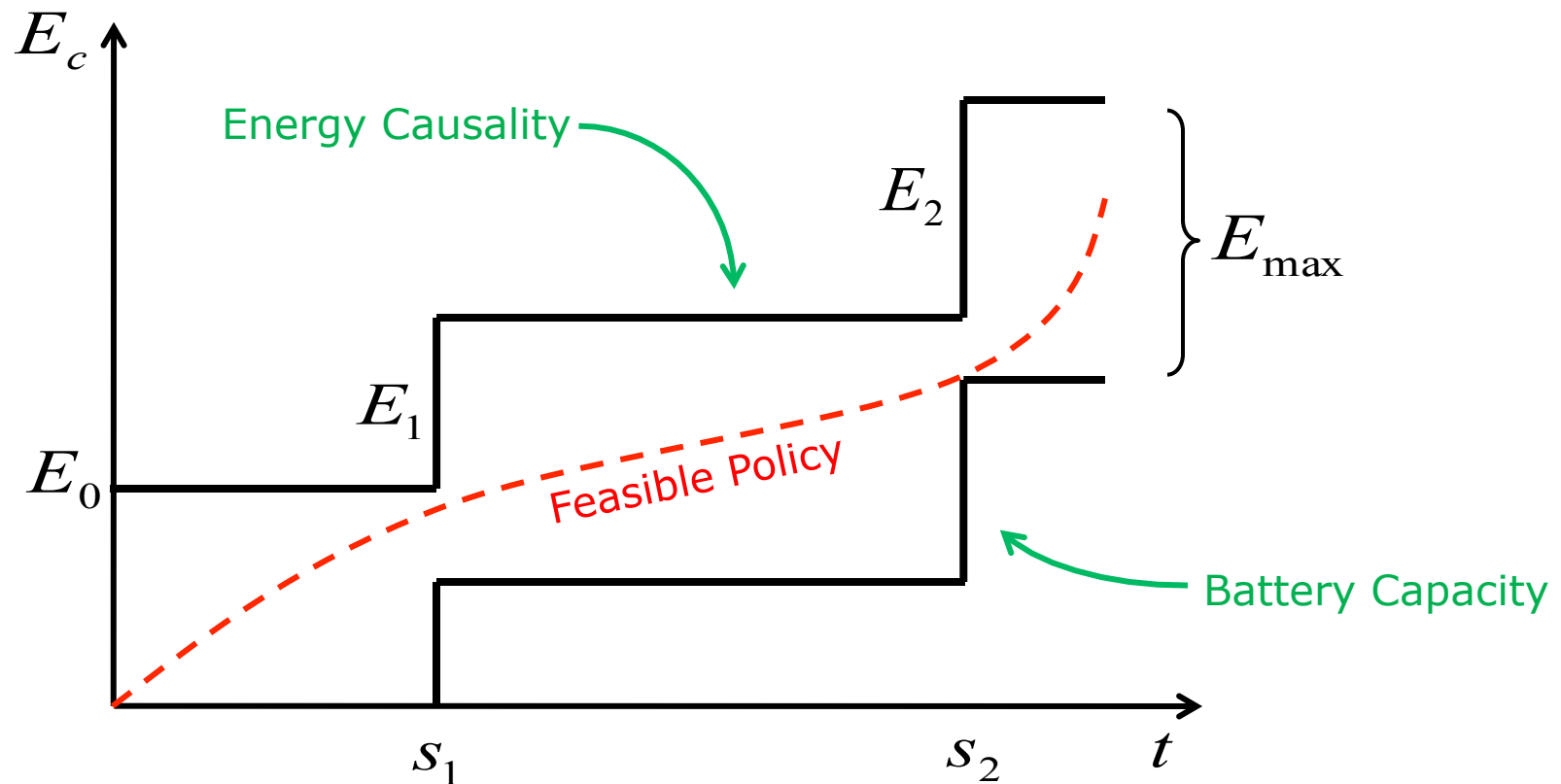
- **Battery Capacity:**  $\sum_{i=0}^{n-1} E_i - \int_0^{t'} p(t) dt \leq E_{\max} \quad s_{n-1} \leq t' \leq s_n$

- **Set of energy-feasible power allocations**

$$\mathfrak{P} = \left\{ p(t) \mid 0 \leq \sum_{i=0}^{n-1} E_i - \int_0^{t'} p(t) dt \leq E_{\max}, \forall n > 0, s_{n-1} \leq t' \leq s_n \right\}$$



# Energy "Tunnel"





# Optimization Problem

- Maximize total number of transmitted bits by deadline  $T$

$$\max_{p(t)} \int_0^T r(p(t)) dt, \quad s.t. \quad p(t) \in \mathfrak{P}$$

$$\mathfrak{P} = \left\{ p(t) \mid 0 \leq \sum_{i=0}^{n-1} E_i - \int_0^{t'} p(t) dt \leq E_{\max}, \forall n > 0, s_{n-1} \leq t' \leq s_n \right\}$$

- Convex** constraint set, **concave** maximization problem



# Necessary conditions for optimality of a transmission policy

- Property 1: **Transmission power remains constant between energy arrivals.**
- Let the total consumed energy in epoch  $[s_i, s_{i+1}]$  be  $E_{total}$  which is available at  $t = s_i$ . Then the power policy

$$p' = \frac{E_{total}}{s_{i+1} - s_i}, \quad t \in [s_i, s_{i+1}]$$

is feasible and better than a variable power transmission;  
shown easily using concavity of  $r(p)$



# Necessary conditions for optimality

- Property 2: Battery never overflows.

Proof:

Assume an energy of  $\Delta$  overflows at time  $\tau$

$$\text{Define } p'(t) = \begin{cases} p(t) + \frac{\Delta}{\delta} & [\tau - \delta, \tau] \\ p(t) & \text{else} \end{cases}$$

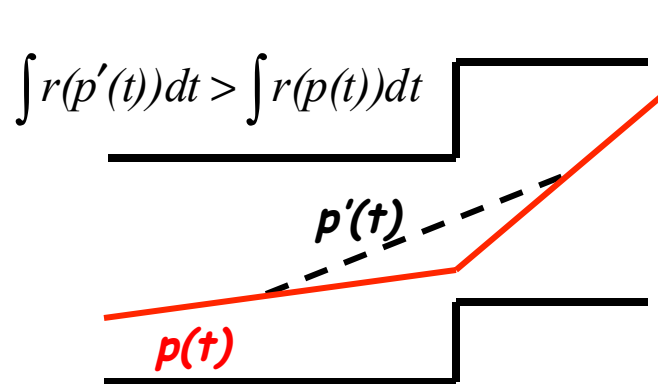
Then  $\int_0^T r(p'(t))dt > \int_0^T r(p(t))dt$  since  $r(p)$  is increasing in  $p$



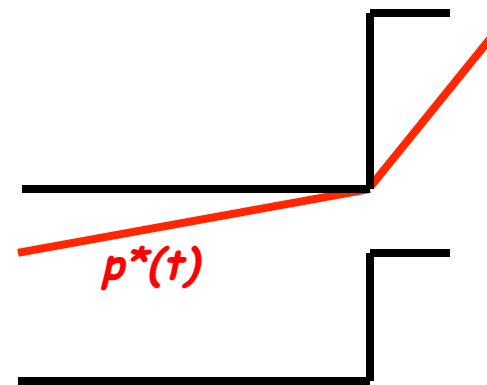


# Necessary conditions for optimality of a transmission policy

- Property 3: Power level increases at an energy arrival instant only if battery is depleted. Conversely, power level decreases at an energy arrival instant only if battery is full.



Policy can be improved

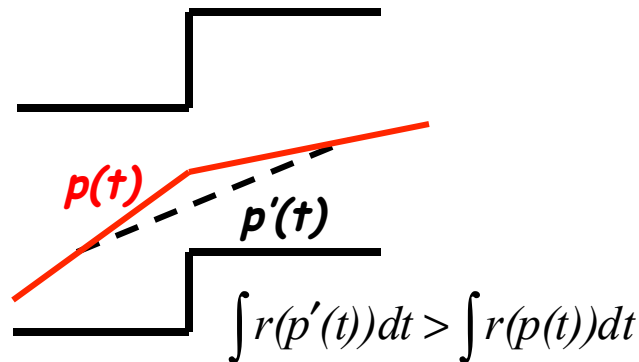


Policy cannot be improved

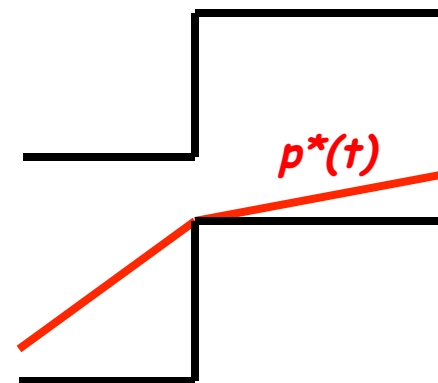


# Necessary conditions for optimality of a transmission policy

- Property 3: Power level increases at an energy arrival instant only if battery is depleted. Conversely, power level decreases at an energy arrival instant only if battery is full.



Policy can be improved



Policy cannot be improved



## Necessary conditions for optimality of a transmission policy

- **Property 4:** Battery is depleted at the end of transmission.

**Proof:** Assume an energy of  $\Delta$  remains after  $p(t)$

$$\text{Define } p'(t) = \begin{cases} p(t) + \frac{\Delta}{\delta} & [T - \delta, T] \\ p(t) & \text{else} \end{cases}$$

$$\text{Then } \int_0^T r(p'(t))dt > \int_0^T r(p(t))dt \quad \text{since } r(p) \text{ is increasing}$$



# Implications of the properties

[Tutuncuoglu-Y. 2012]

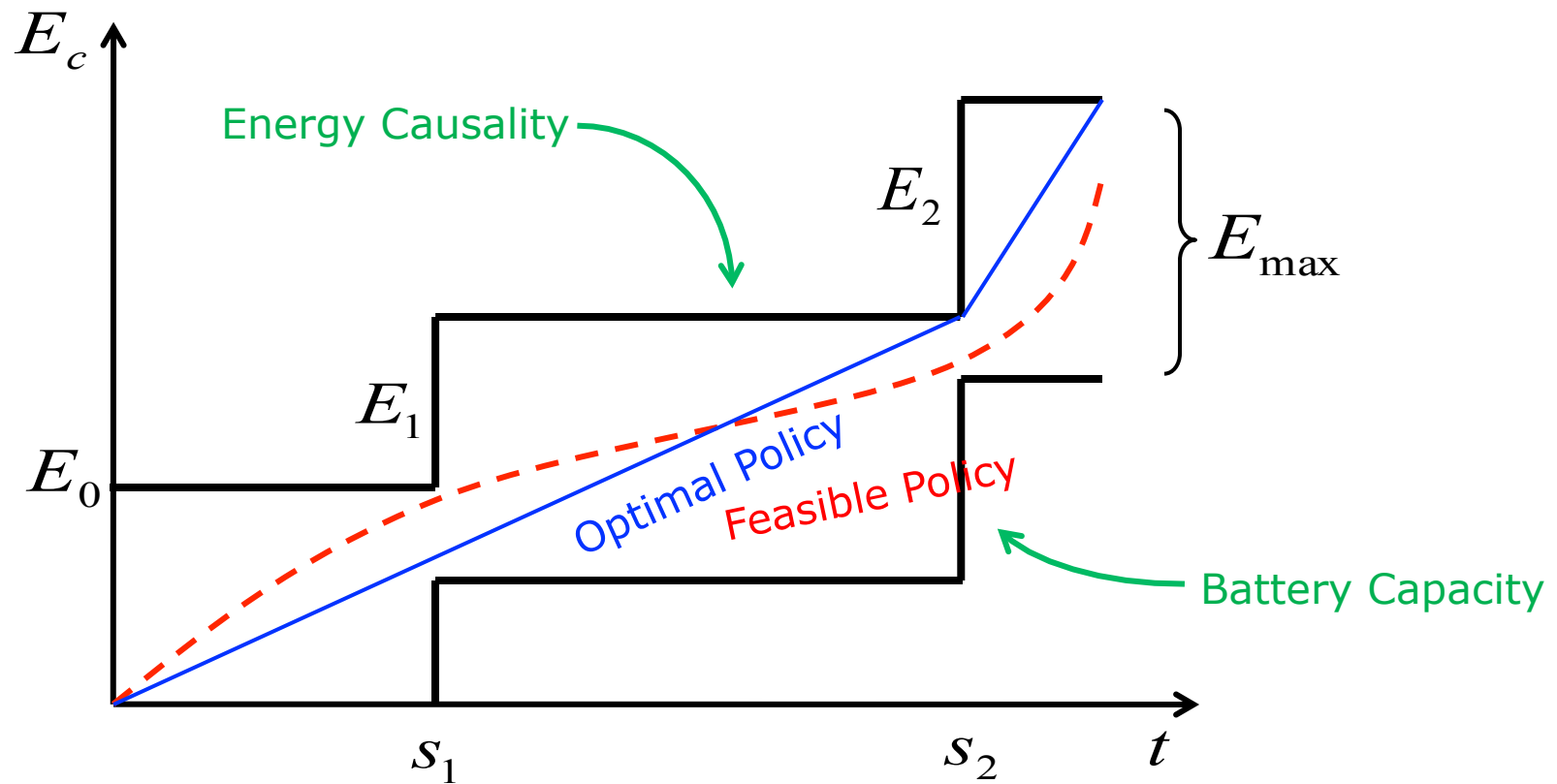
- Structure of optimal policy is piece-wise linear.

$$p(t) = \begin{cases} p_n & i_{n-1} < t < i_n \\ 0 & t > T \end{cases}, \quad i_n \in \{s_n\}, \quad p_n \text{ constant}$$

- For power to increase or decrease, policy must meet the upper or lower boundary of the tunnel respectively.
- At termination step, battery is depleted.
- Utilizing this structure, a recursive algorithm emerges to find the unique optimum policy [Tutuncuoglu-Y. 2012].



# Energy "Tunnel"





# Shortest Path Interpretation

- Optimal policy is identical for any concave power-rate function!
- Let  $r(p) = -\sqrt{p^2 + 1}$ , then the problem solved becomes:

$$\max_{p(t)} \int_0^T -\sqrt{p^2(t) + 1} dt \quad s.t. \quad p(t) \in \mathfrak{P}$$

$$= \min_{p(t)} \underbrace{\int_0^T \sqrt{p^2(t) + 1} dt}_{\text{length of policy path in energy tunnel}} \quad s.t. \quad p(t) \in \mathfrak{P}$$

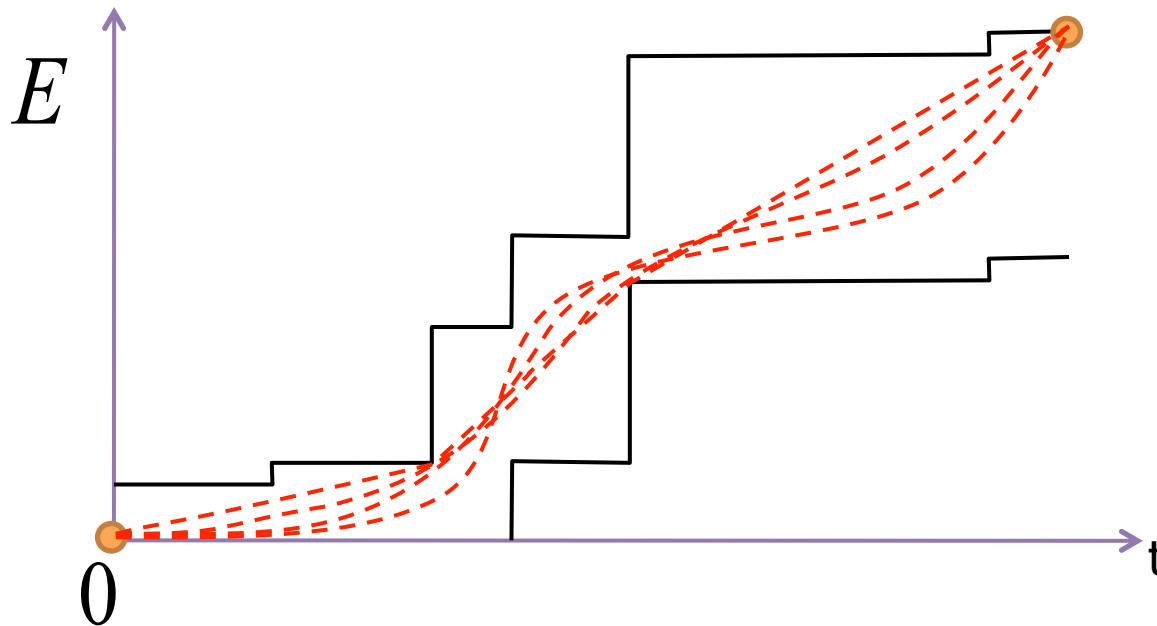
**length** of policy path in energy tunnel

⇒ The **throughput maximizing policy** yields the **shortest path** through the energy tunnel for any concave power-rate function.



# Shortest Path Interpretation

- **Property 1:** Constant power is better than any other alternative
- **Shortest path** between two points is a line (constant slope)







# Alternative Solution (Using Property 1)

- Transmission power is constant within each epoch:

$$p(t) = \{p_i, t \in \text{epoch } i, i = 1, \dots, N\}$$

( $N$ : Number of arrivals within  $[0, T]$ )

$$\max_{p_i} \sum_{i=1}^N L_i \cdot r(p_i)$$

( $L_i$ : length of epoch  $i$ )

$$s.t. \quad 0 \leq \sum_{i=1}^n E_i - L_i p_i \leq E_{\max} \quad n = 1, \dots, N$$

- KKT conditions  $\rightarrow$  optimum power policy.



# Solution

## ■ Complementary Slackness

Conditions:

$$\lambda_n \left( \sum_{i=1}^n L_i p_i - E_i \right) = 0 \quad \forall n$$

$$\mu_n \left( \sum_{i=1}^n E_i - L_i p_i - E_{\max} \right) = 0 \quad \forall n$$

$\lambda_n$ 's are positive only when battery is empty  $\left( \sum_{i=1}^n L_i p_i - E_i \right) = 0$

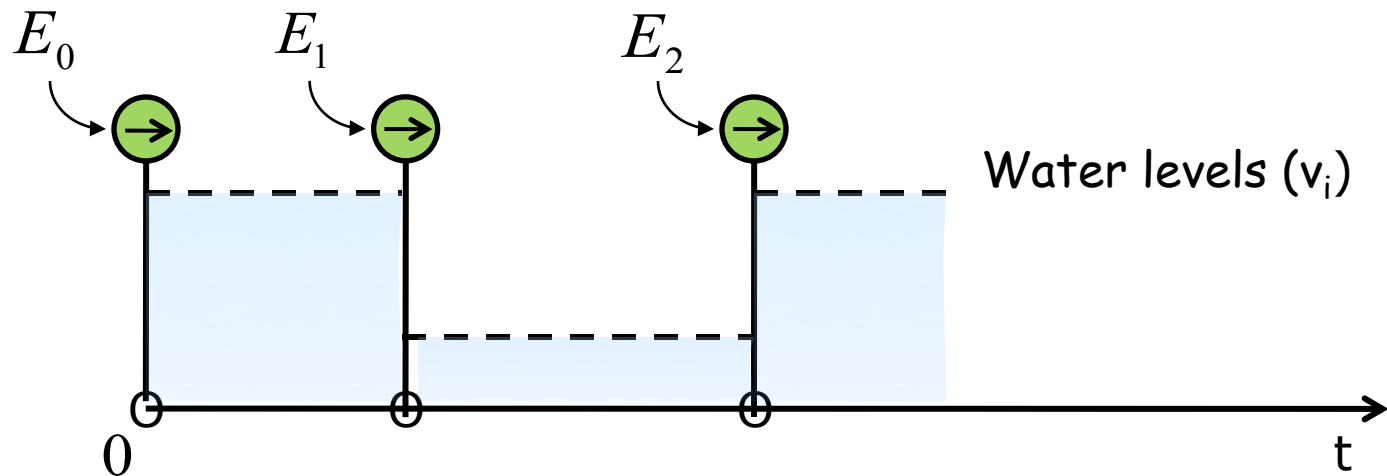
$\mu_n$ 's only positive only when battery is full  $\left( \sum_{i=1}^n E_i - L_i p_i - E_{\max} \right) = 0$

$$p_n^* = \left[ \frac{1}{\sum_{j=n}^N (\lambda_j - \mu_j)} - 1 \right]^+ \quad \begin{array}{l} \text{increases with positive } \lambda_n \\ \text{decreases with positive } \mu_n \end{array}$$



# Directional Water-Filling

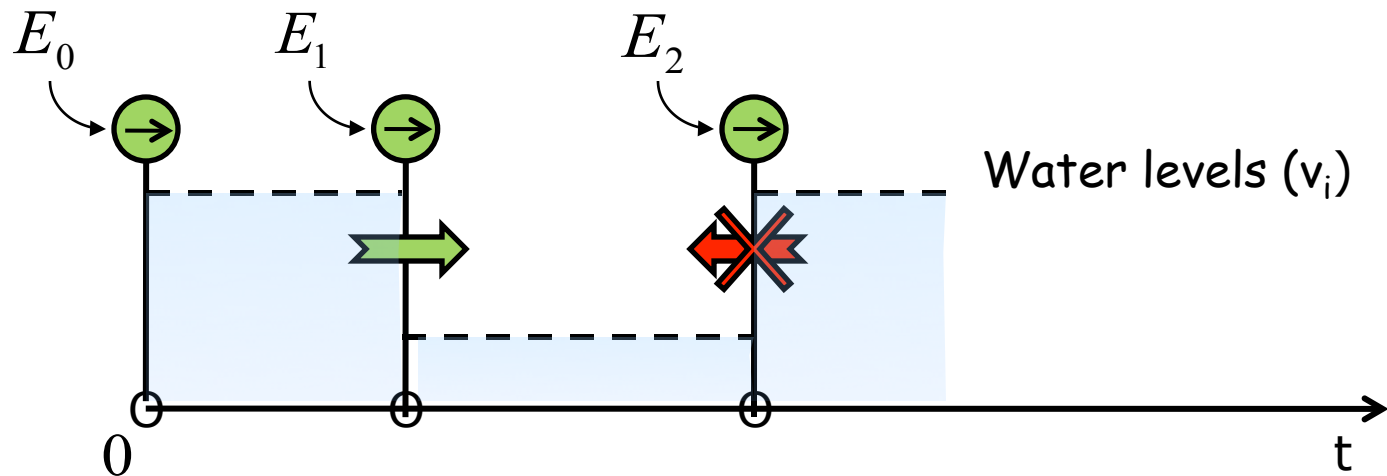
- [Ozel, Tutuncuoglu, Ulukus, Y., 2011]
- Harvested energies filled into epochs individually





# Directional Water-Filling

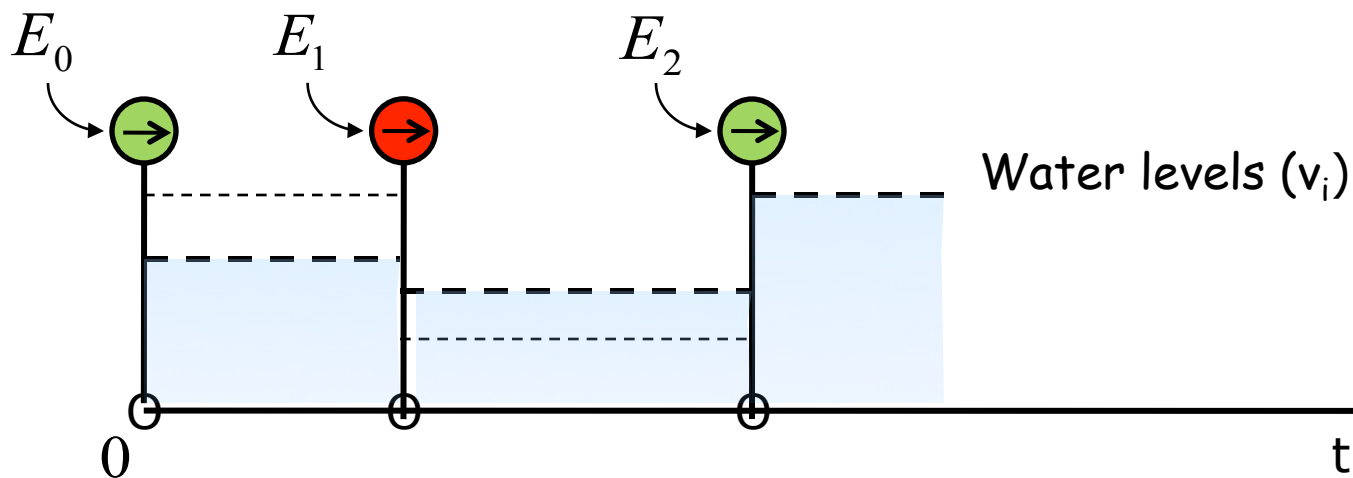
- Harvested energies filled into epochs individually
- Constraints:
  - Energy Causality:** water-flow only forward in time ➡





# Directional Water-Filling

- Harvested energies filled into epochs individually
- Constraints:
  - **Energy Causality:** water-flow only forward in time
  - **Battery Capacity:** water-flow limited to  $E_{max}$  by taps  $\rightarrow$

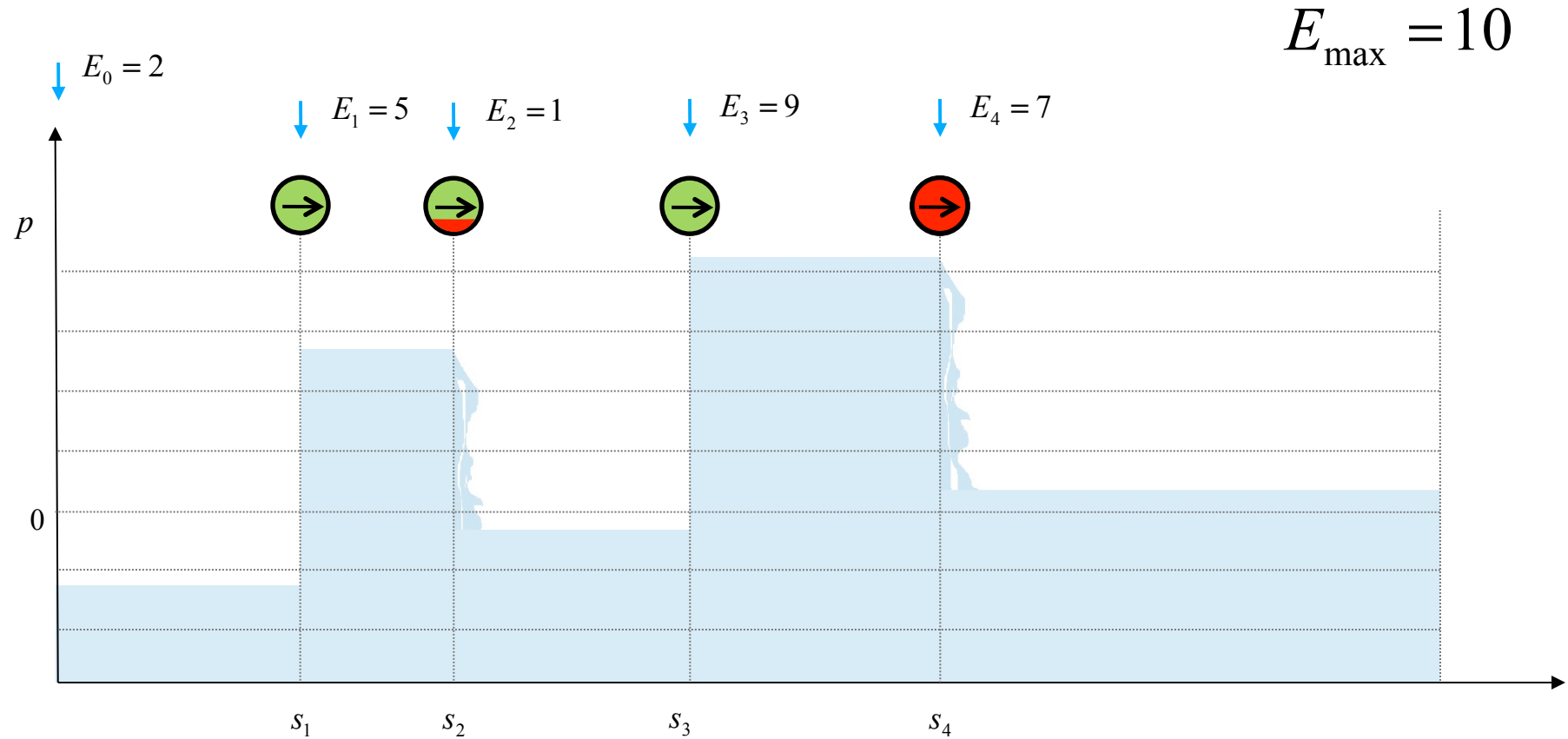




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# Example

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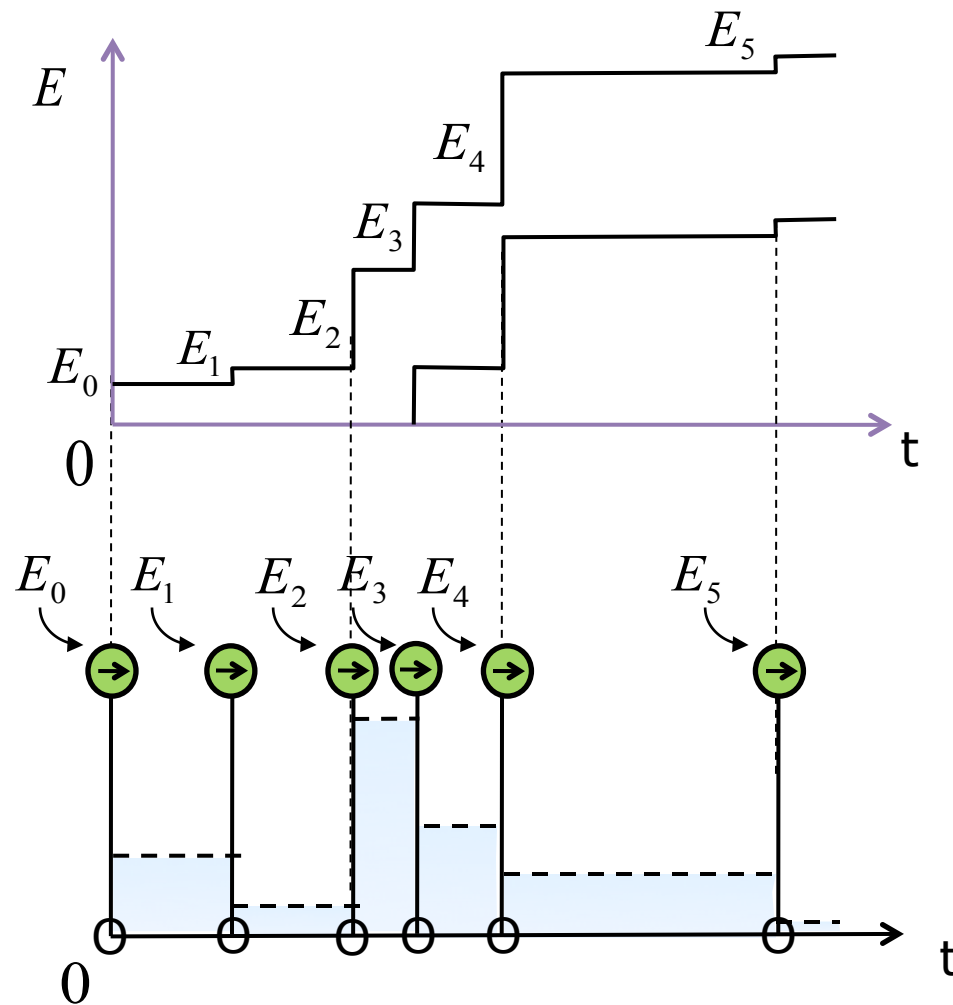


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# Directional Water-Filling

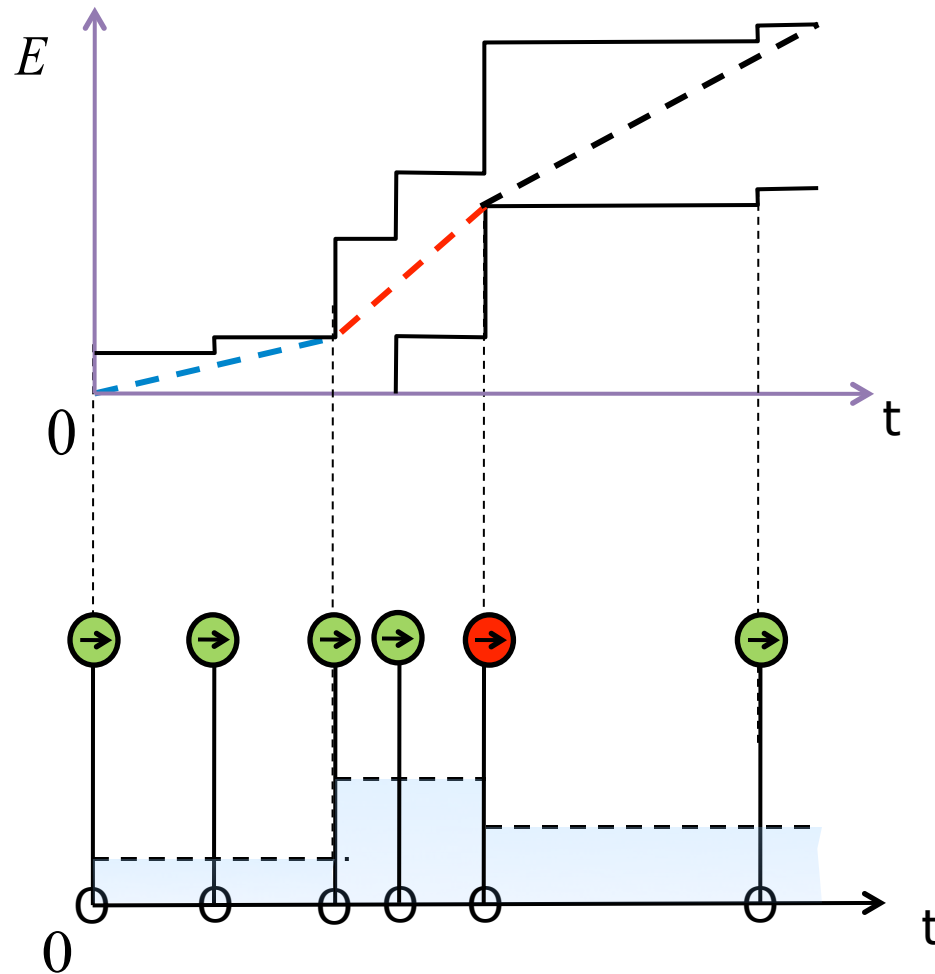


- Energy tunnel and directional water-filling approaches yield the same policy





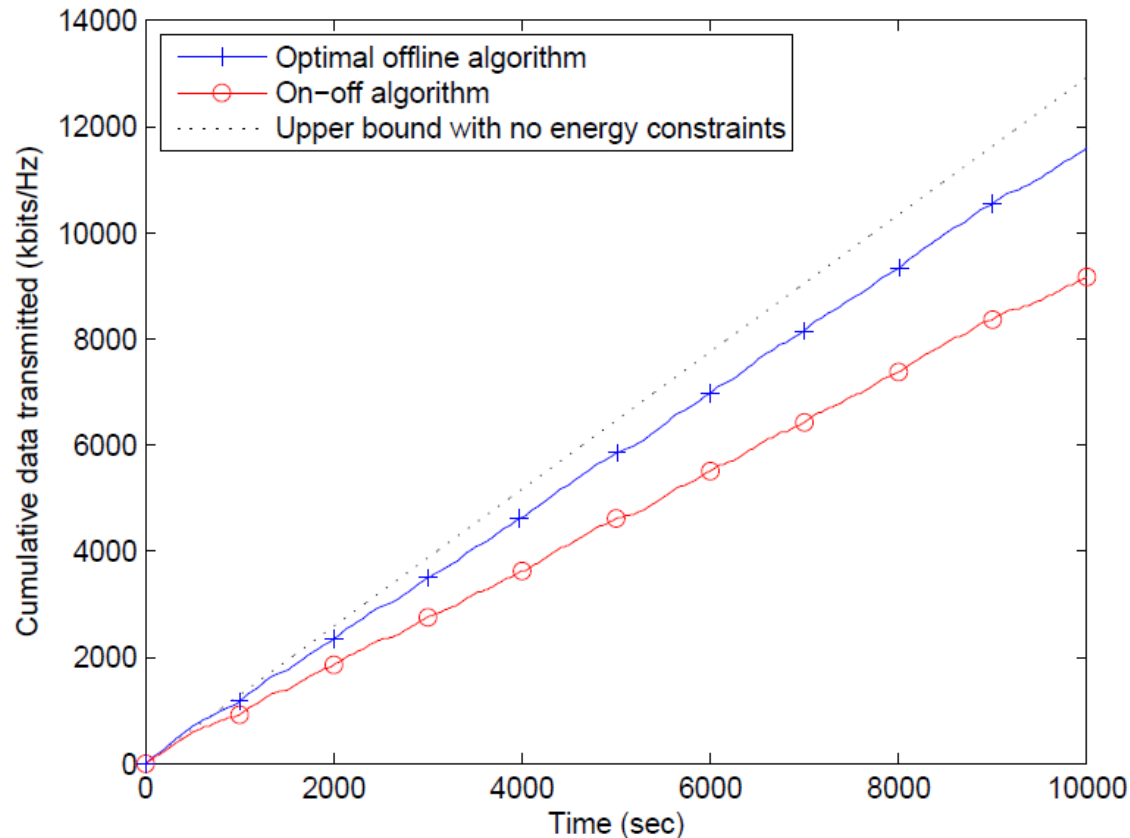
# Directional Water-Filling



- Energy tunnel and directional water-filling approaches yield the same policy



# Simulation Results

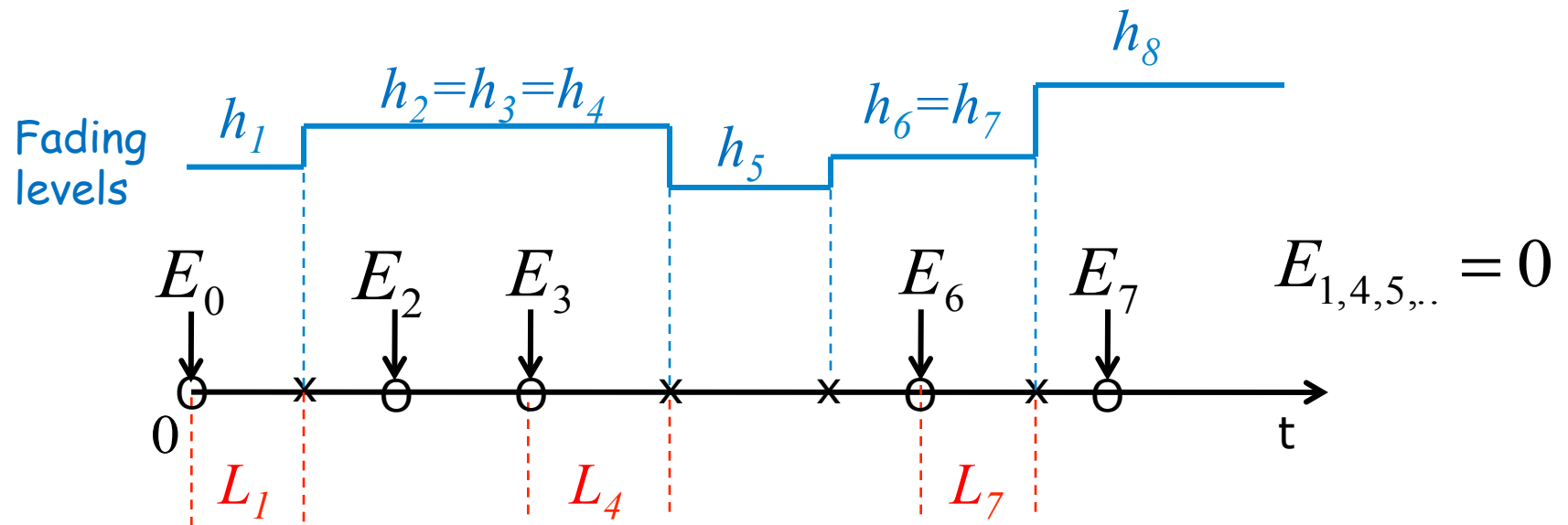


- Improvement of optimal algorithm over an *on-off transmitter* in a simulation with truncated Gaussian arrivals.



# Fading Channels

[Ozel-Tutuncuoglu-Ulukus-Y.'11]

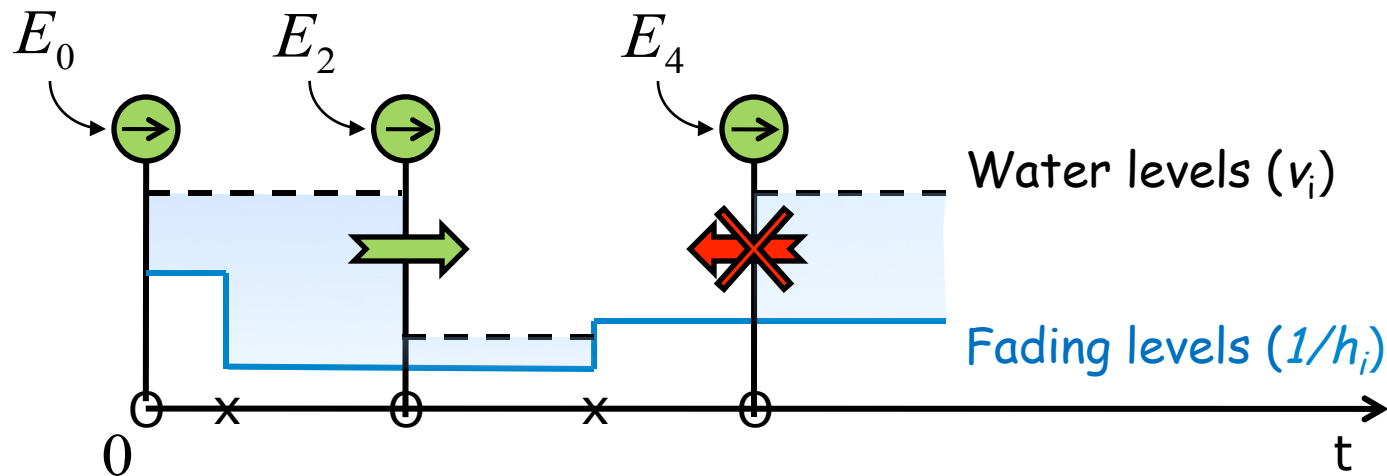


- AWGN Channel with fading  $h$ :  $r(p, h) = \frac{1}{2} \log(1 + hp)$
- Each "epoch" defined as the interval between two "events".



# Directional Water-Filling for Fading Channels

- Same directional water filling with base levels adjusted according to channel quality.
- Directional water flow (Energy causality)
- Limited water flow (Battery capacity)





# Transmission Completion Time Minimization (TCTM)

- Given the total number of bits to send as  $B$ , complete transmission in the shortest time possible.

$$\min_{p(t)} T \quad s.t. \quad B - \int_0^T r(p(t)) dt \leq 0, \quad p(t) \in \mathfrak{P}$$

$$\mathfrak{P} = \left\{ p(t) \mid 0 \leq \sum_{k=0}^{n-1} E_k - \int_0^{t'} p(t) dt \leq E_{\max}, \forall n > 0, s_{n-1} \leq t' \leq s_n \right\}$$



# Relationship of STTM and TCTM

- Lagrangian dual of TCTM problem becomes:

$$\begin{aligned} & \max_{u \geq 0} \left( \min_{p(t) \in \mathfrak{P}, T} T + u \left( B - \int_0^T r(p(t)) dt \right) \right) \\ &= \max_{u \geq 0} \left( \min_T \left( T + uB - u \underbrace{\max_{p(t) \in \mathfrak{P}} \int_0^T r(p(t)) dt}_{\text{STTM problem for deadline } T} \right) \right) \end{aligned}$$



# Relationship of STTM and TCTM

- Optimal allocations are identical:

STTM's solution  
for deadline  $T$   
departing  $B$  bits



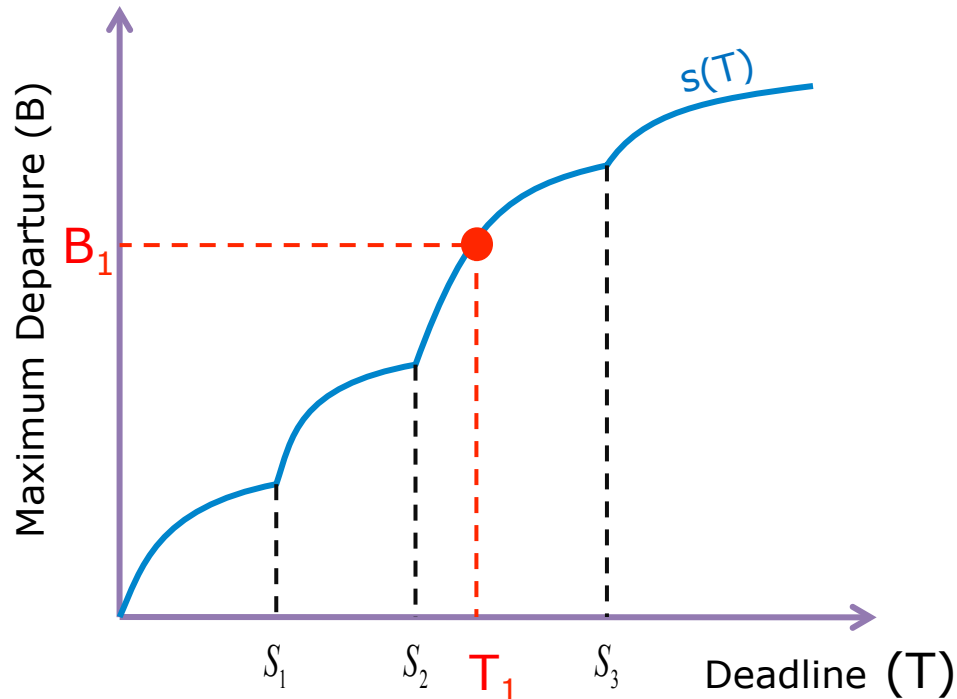
TCTM's solution  
for departing  $B$   
bits in time  $T$

- STTM solution can be used to solve the TCTM problem



# Maximum Service Curve

- Continuous, monotone increasing, invertible



- Optimal allocation for TCTM with  $B_1$  bits

=

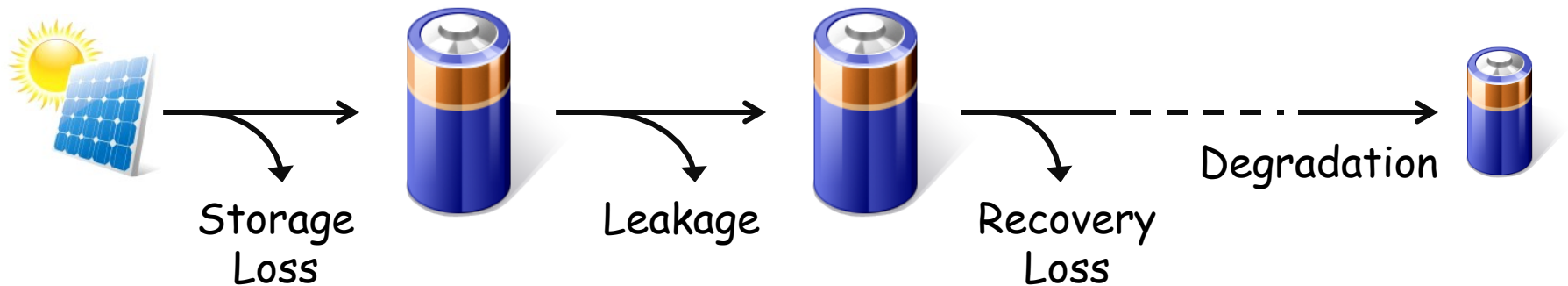
Optimal allocation for STTM with deadline  $T_1$





# Transmission Policies with Inefficient Energy Storage

- Energy stored in a battery, supercapacitor, . . .
- “Real life” issues:

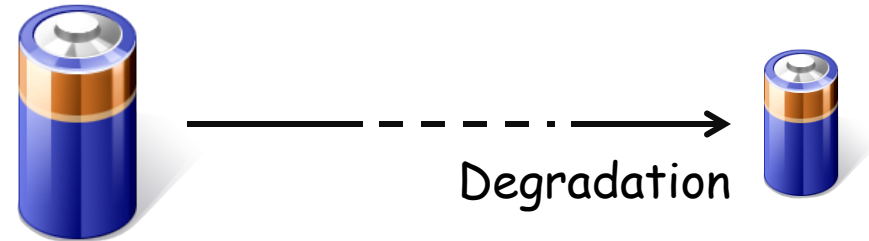


- [Devillers-Gunduz '12]: Leakage and Degradation
- [Tutuncuoglu-Y.-Ulukus '15]: Storage/Retriaval Losses

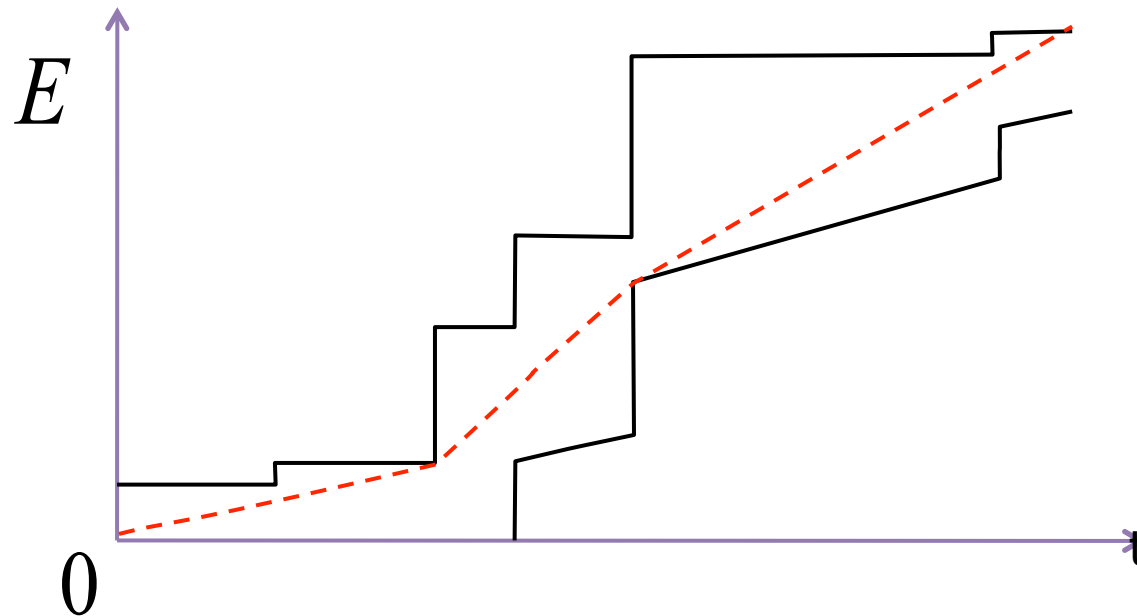


# Battery Degradation

- [Devillers-Gunduz '12]



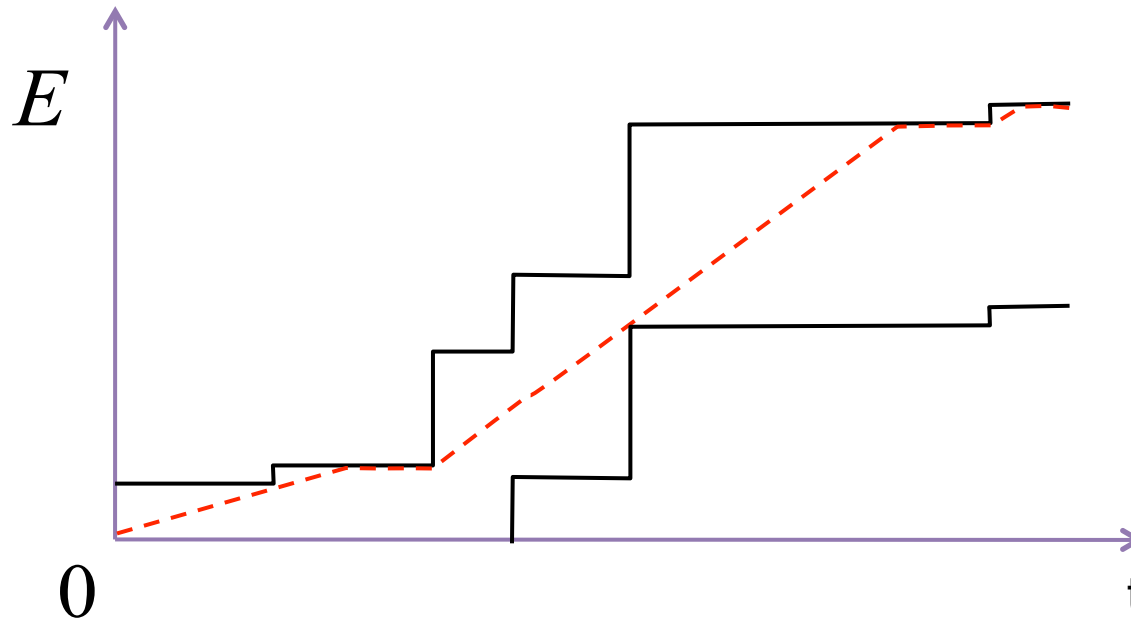
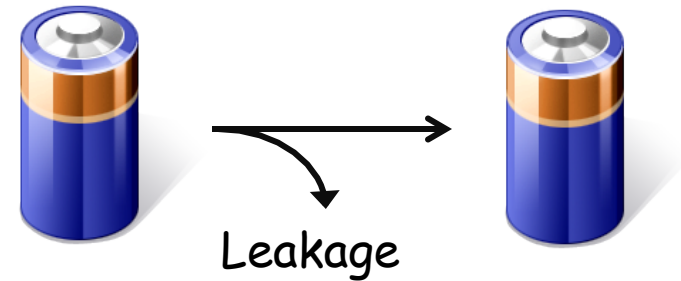
- **Optimal Policy:** Shortest path within **narrowing tunnel**





# Battery Leakage

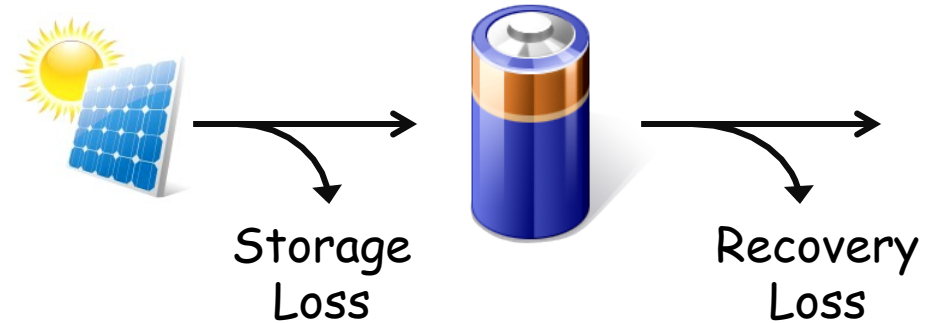
- [Devillers-Gunduz '12]
- **Optimal Policy:** When total energy in an epoch is low, deplete energy earlier to reduce leakage.



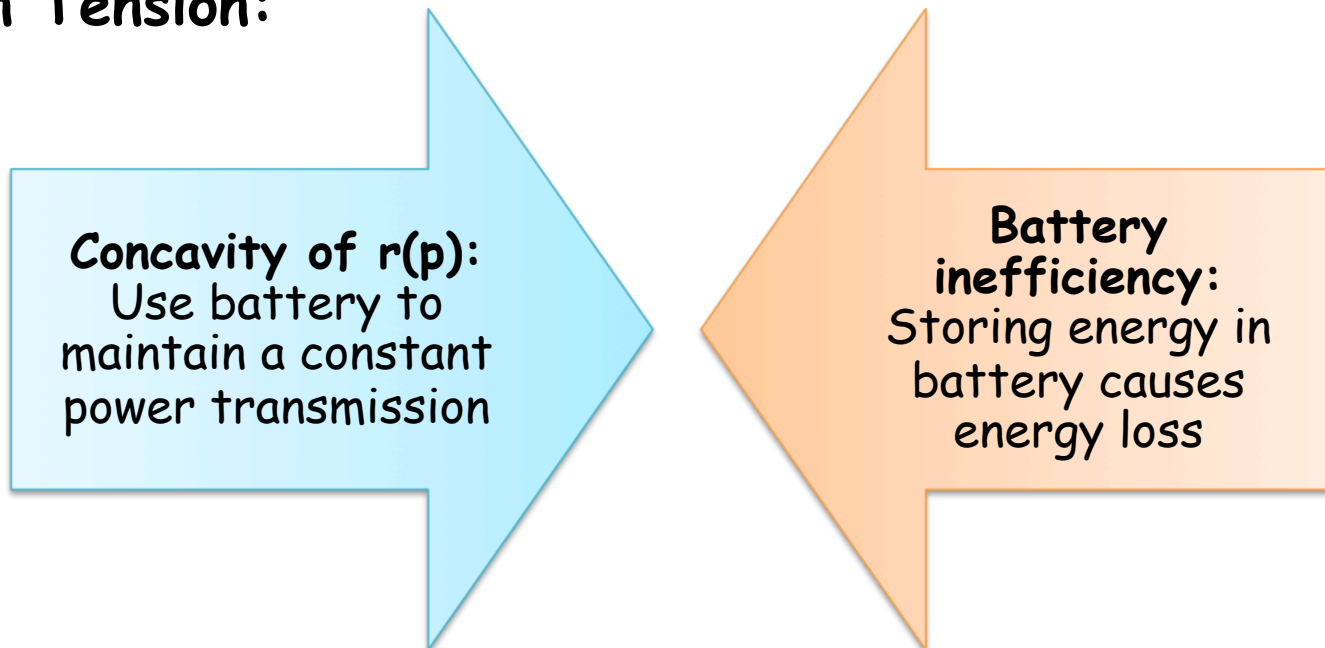


# Storage/Recovery Losses

- [Tutuncuoglu-Y.-Uluks '15]

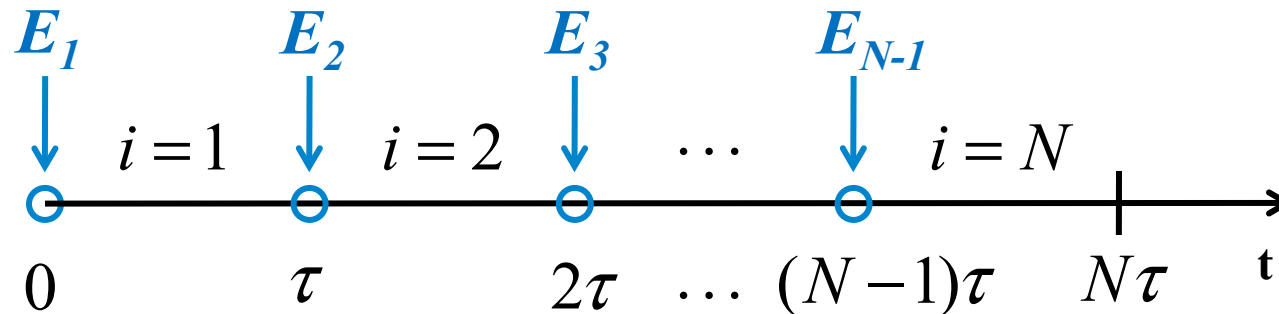


- Main Tension:**





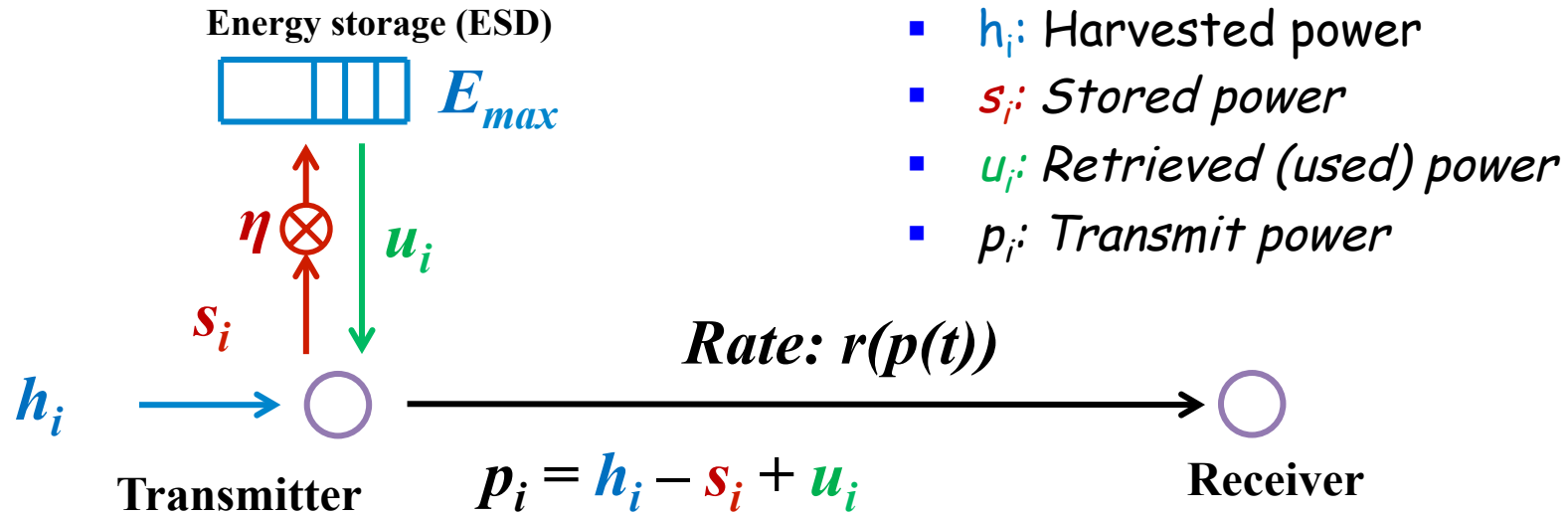
# Time slotted model



- **Time slots** of duration  $\tau = 1 \text{ s}$
- **Energy harvests:** Size  $E_i$  at the beginning of time slot  $i$



# System Model



- ESD has finite capacity  $E_{max}$  and storage efficiency  $\eta$ .

- **Energy Causality:** 
$$\sum_{n=1}^i \eta s_n - u_n \geq 0, \quad i = 1, \dots, N$$

- **Storage Capacity:** 
$$\sum_{n=1}^i \eta s_n - u_n \leq E_{max}, \quad i = 1, \dots, N$$



# Throughput Maximization

- Find optimal energy storage policy that maximizes the average throughput of an energy harvesting transmitter within a deadline of  $N$  time slots.

$$\begin{aligned} \max_{\{s_i, r_i\}} \quad & \sum_{i=1}^N r(E_i - s_i + u_i) \\ \text{s.t.} \quad & 0 \leq E_0 + \sum_{n=1}^i (\eta s_n - u_n) \leq E_{\max}, \quad i = 1, \dots, N, \\ & E_i - s_i + u_i \geq 0, \quad s_i \geq 0, \quad u_i \geq 0, \quad i = 1, \dots, N. \end{aligned}$$



# Throughput Maximization

Old problem:

$$\begin{aligned} \max_{\{p_i\}} \quad & \sum_{i=1}^N r(p_i) \\ \text{s.t.} \quad & 0 \leq \sum_{n=1}^i (E_i - p_i) \leq E_{\max}, \quad i = 1, \dots, N, \\ & p_i \geq 0, \quad i = 1, \dots, N. \end{aligned}$$

$$\begin{aligned} \max_{\{s_i, r_i\}} \quad & \sum_{i=1}^N r(E_i - s_i + u_i) \\ \text{s.t.} \quad & 0 \leq \sum_{n=1}^i (\eta s_i - u_i) \leq E_{\max}, \quad i = 1, \dots, N, \\ & E_i - s_i + u_i \geq 0, \quad s_i \geq 0, \quad u_i \geq 0, \quad i = 1, \dots, N. \end{aligned}$$



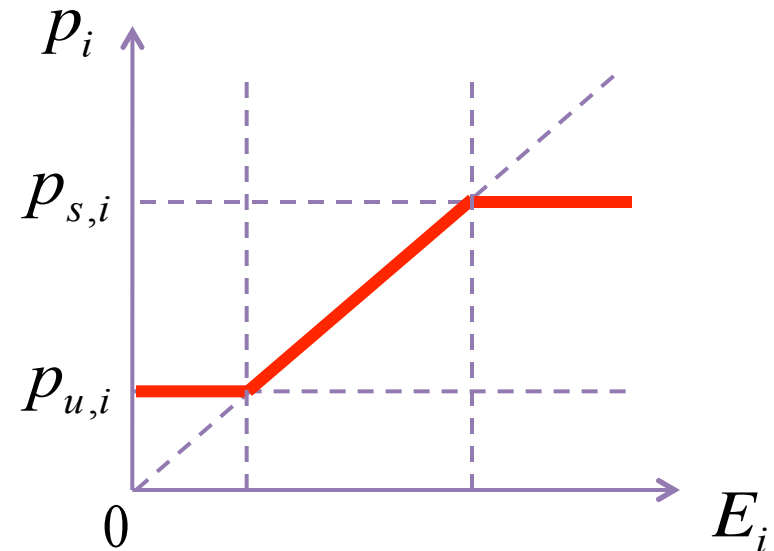


# Optimal Power Policy

- Structure of optimal policy:

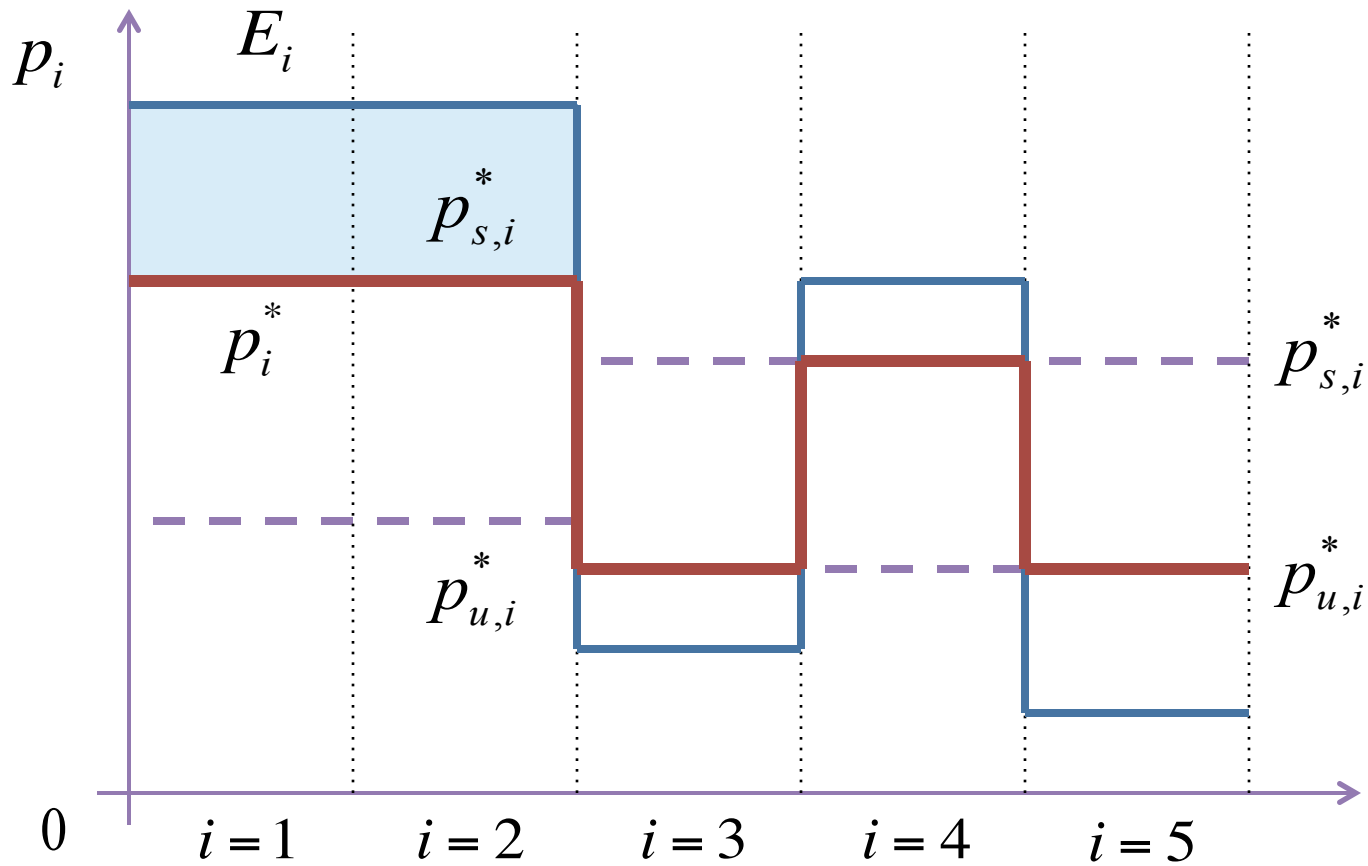
$$p_i = \begin{cases} [p_{s,i}]^+ & E_i \geq p_{s,i} \\ E_i & p_{u,i} \leq E_i \leq p_{s,i} \\ p_{u,i} & E_i \leq p_{u,i} \end{cases}$$

“Double Threshold Policy”



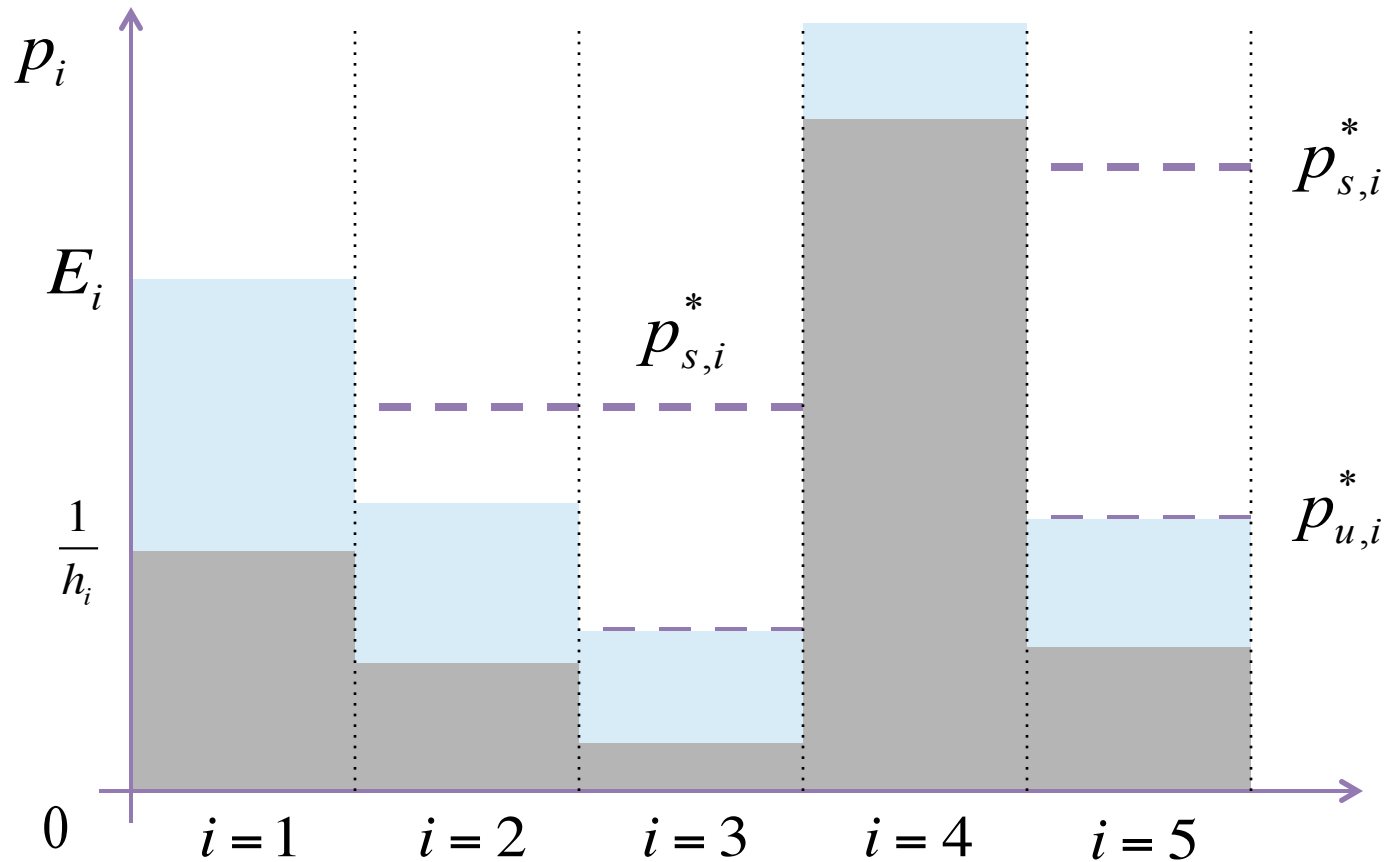


# Optimal Power Policy





# Optimal Power Policy (Fading channel)





# Optimal Online Policy

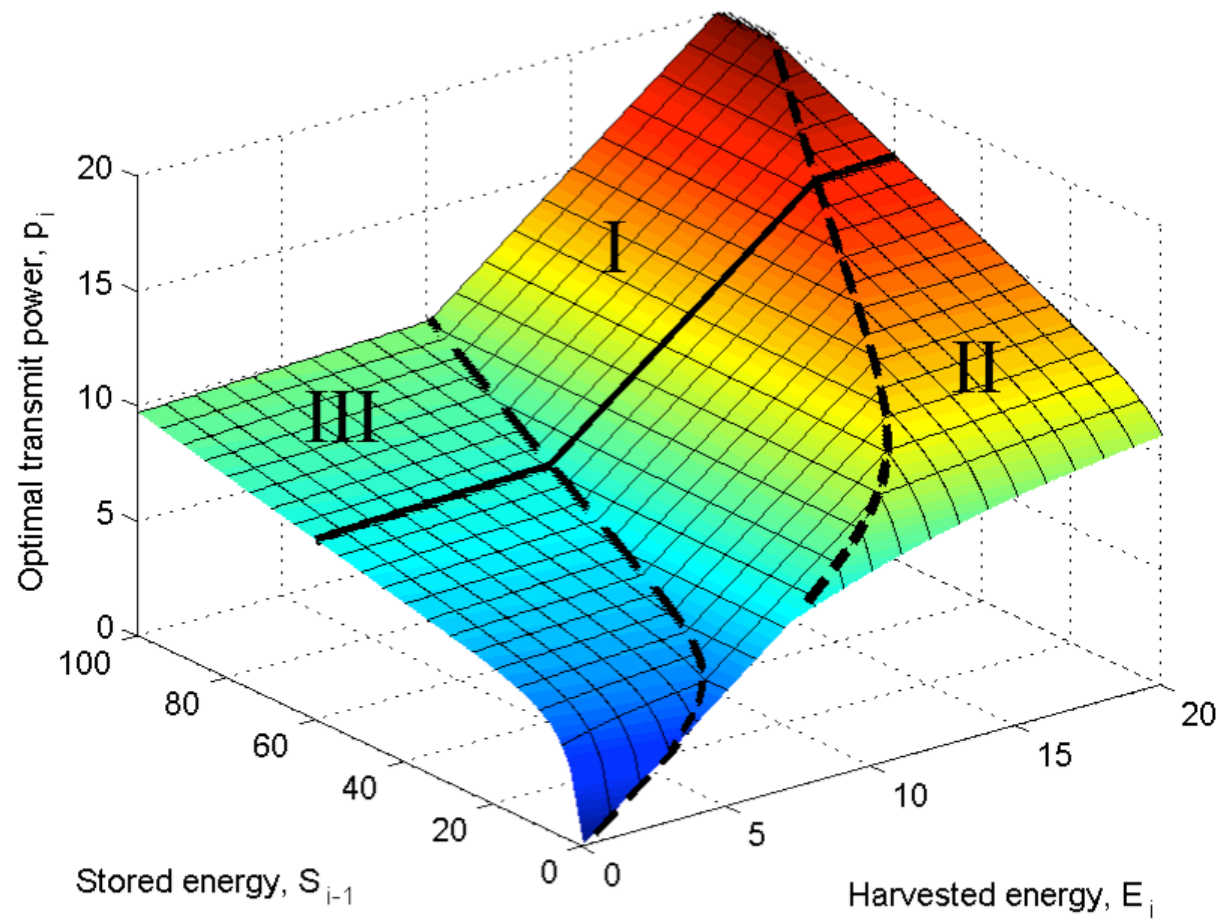
- So far, we have discussed **offline** policies.
- Energy harvesting scenario may not be predictable, or may not be available prior to transmission
- **Markov Decision Process (MDP)** formulation:

- Action:  $p_i = g_i(E^i, h^i)$

- Value: 
$$J_i(E^i, h^i) = \max_{\pi_i} r(g_i(E^i, h^i), h_i) + \mathbf{E} \left[ \sum_{n=i+1}^N r(g_i(E^i, h^i), h_i) \right]$$
$$= \max_{\pi_i} r(g_i(E^i, h^i), h_i) + \mathbf{E} [J_{i+1}(E^{i+1}, h^{i+1})]$$



# Optimal Online Policy





# Proposed Online Policy

- Both offline and online policies point to **thresholds**
- Choose **fixed thresholds** throughout transmission

$$p_i = \begin{cases} \max\{p_s, E_i + S_i - E^{\max}\} & E_i \geq p_s \\ E_i & p_u \leq E_i \leq p_s \\ \min\{p_u, E_i + S_i\} & E_i \leq p_u \end{cases}$$

to satisfy

$$\eta \int_{p_s}^{\infty} (e - p_s) p_E(e) de - \int_0^{p_u} (p_u - e) p_E(e) de = 0$$



# Simulations

$N = 10^4$  time slots

$\tau = 10$  ms

$E_{\max} = 1$  mJ

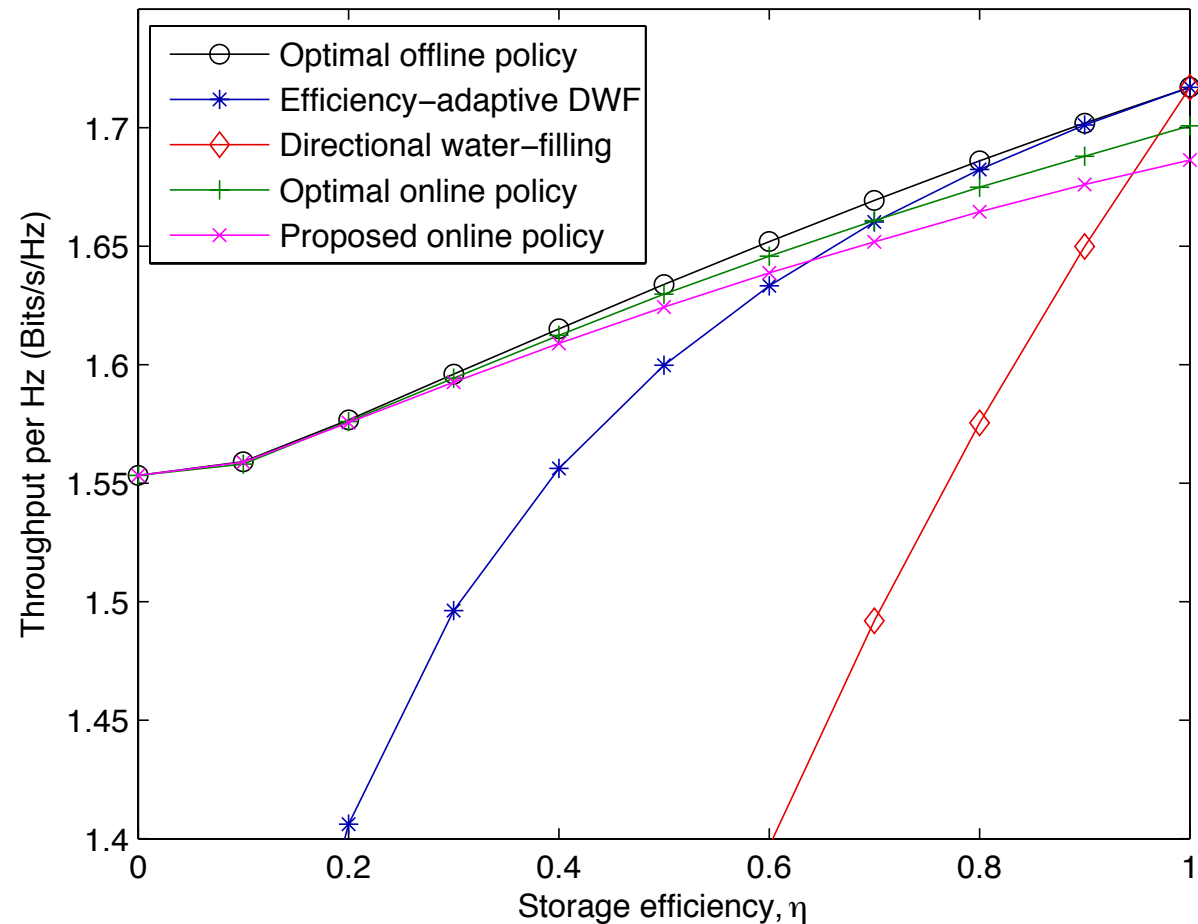
$E_0 = 0$

$E_i \sim i.i.d. U[0, 200] \mu J$

$h = -100$  dB

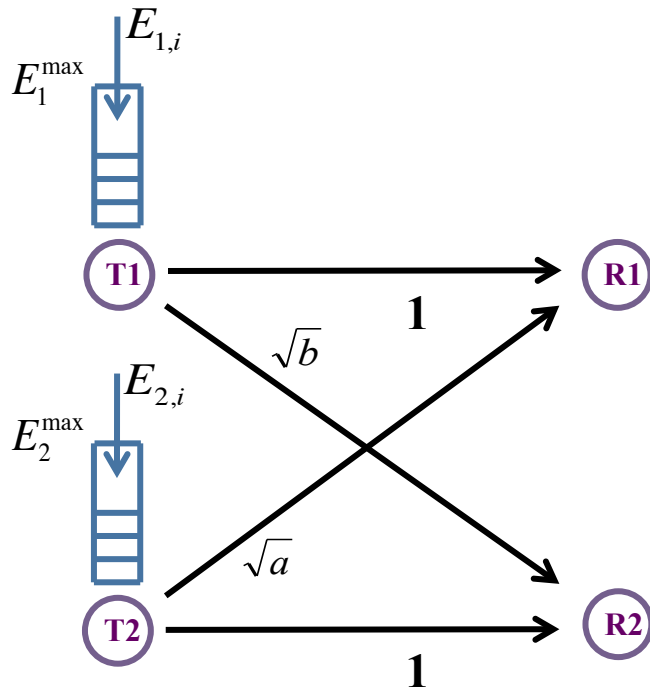
$B = 1$  MHz

$N_0 = 10^{-19}$  W/Hz





# Multiple EH Transmitters

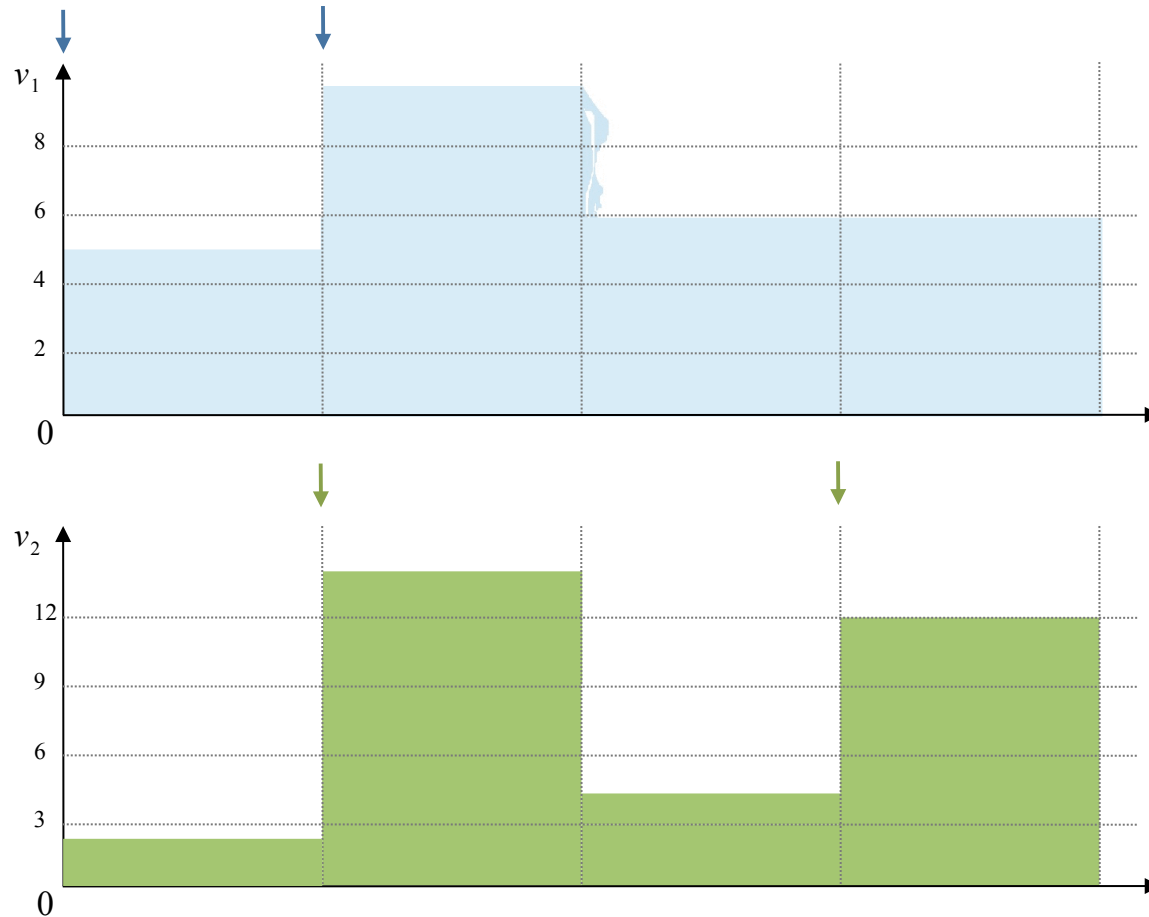


- How to transmit when there are **more than one energy harvesting transmitters** sharing the same medium?
- Many multi-node models, e.g.,
  - MAC and BC [Ozel-Yang-Ulukus '11,'12],
  - Relay [Cui-Zhang '12], [Oner-Erkip '13]
  - Two-way Relay Ch. [Tutuncuoglu-Varan-Yener '15],
  - Interference Channel [Tutuncuoglu-Yener '12]





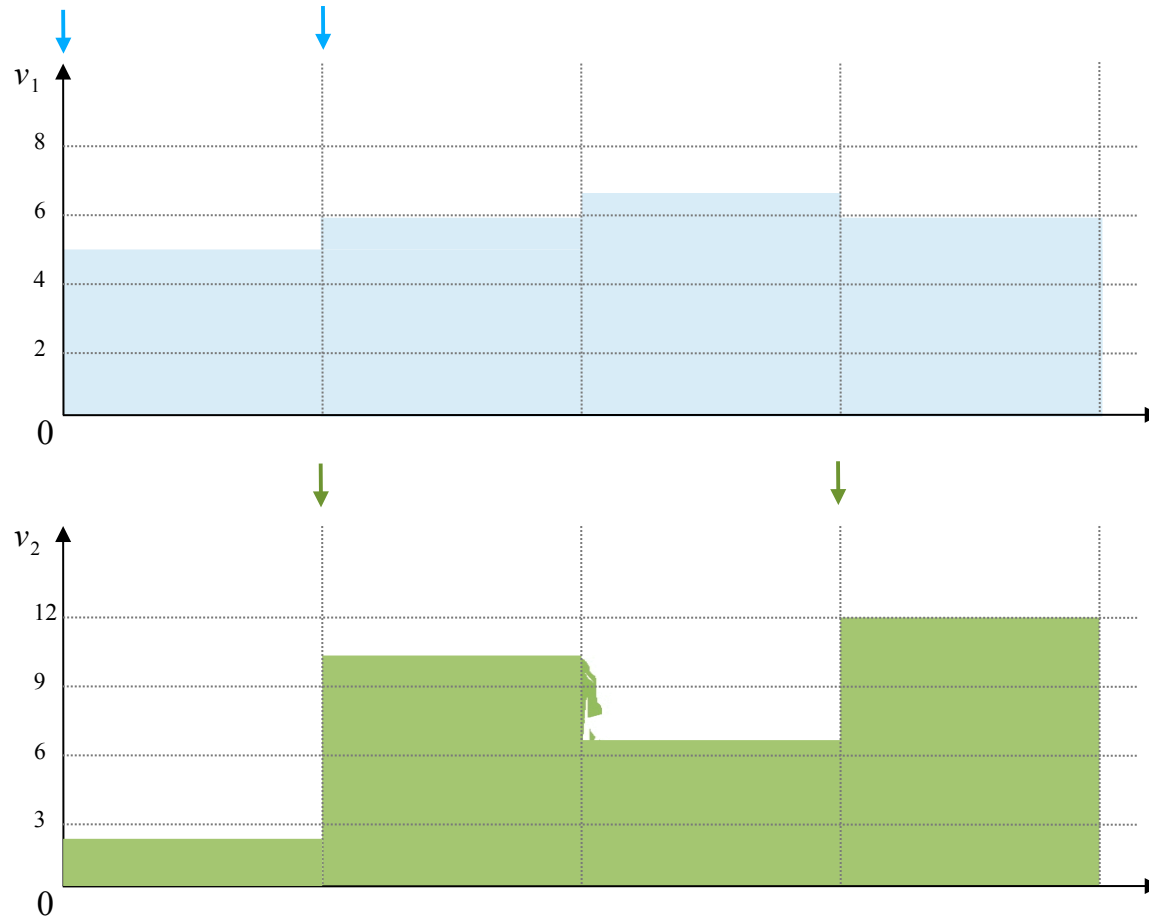
# Iterative Generalized Directional Water-filling (IGDWF)



GDWF for  
User 1



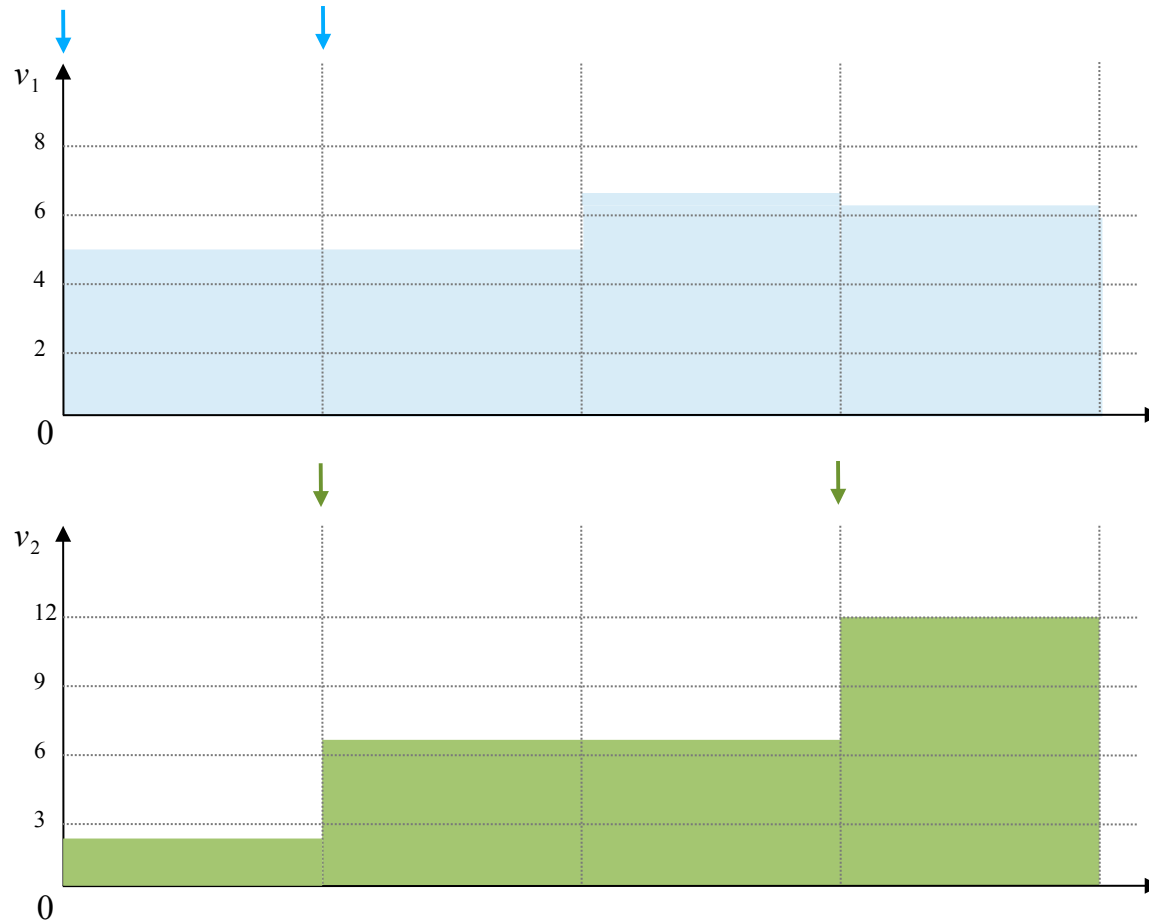
# Iterative Generalized Directional Water-filling (IGDWF)



GDWF for  
User 2



# Iterative Generalized Directional Water-filling (IGDWF)

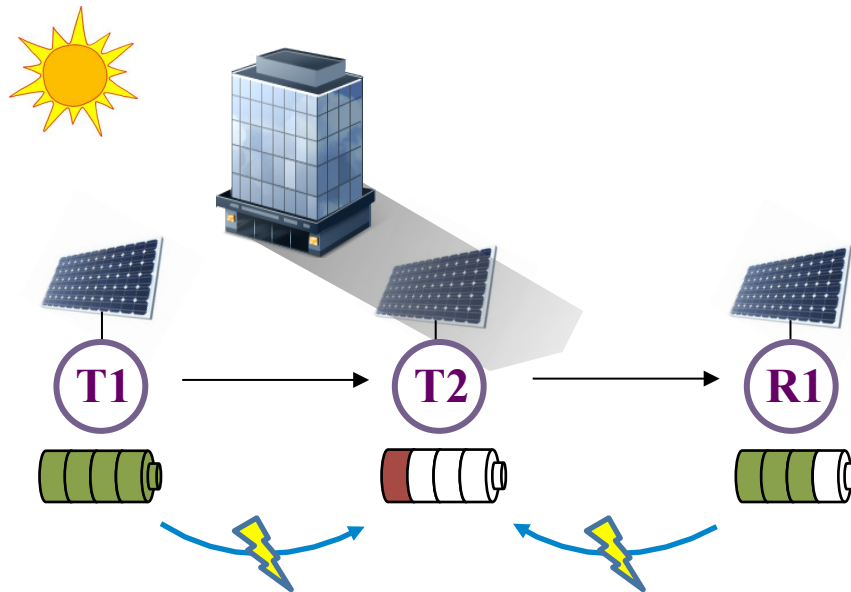


GDWF for  
User 1



# Multiple EH Transmitters: Energy Cooperation

- Intermittent energy  $\Rightarrow$  nodes may be energy deprived!



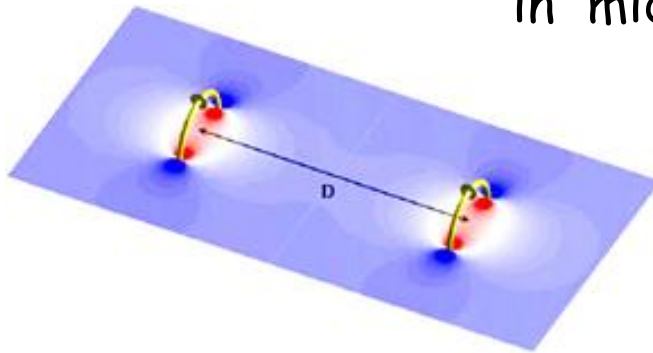
- Energy cooperation between nodes can be very useful!
- [Gurakan-Ozel-Ulukus '12]
- [Tutuncuoglu-Y. '13]



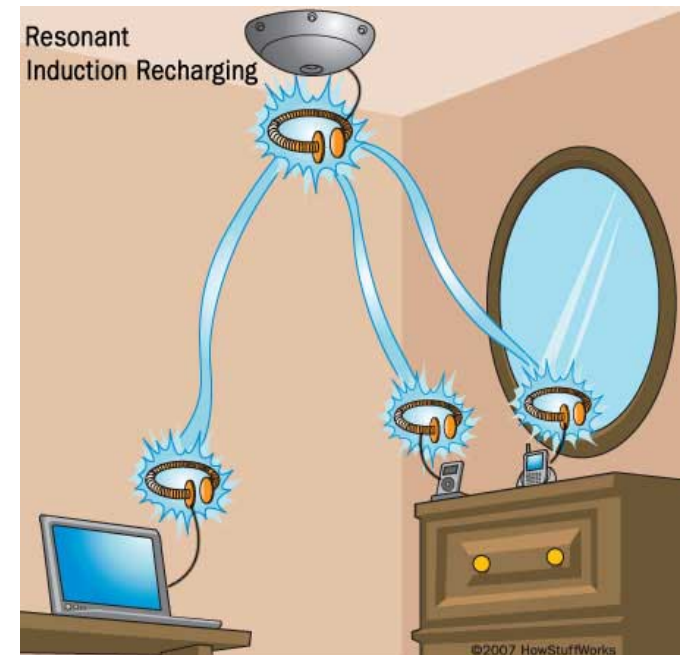
# Wireless Energy Transfer



- Already present in RFID systems
- New technologies like **strongly coupled magnetic resonance** reported to achieve high efficiency in mid-range



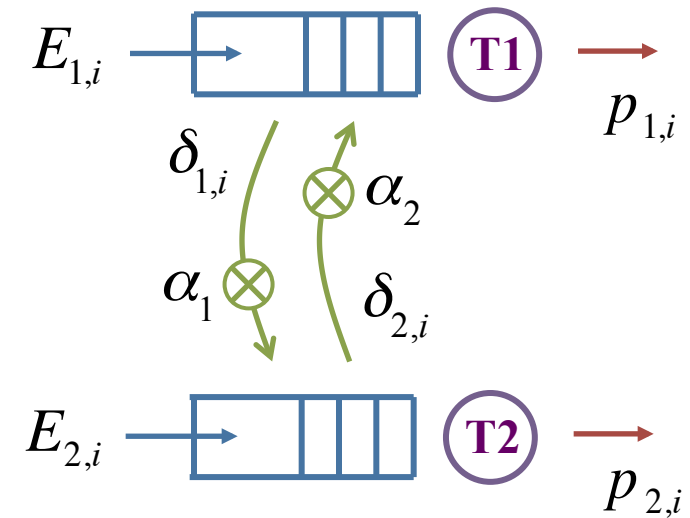
- 50 percent efficiency at 6 feet (MIT)
- 90 percent efficiency at 3 feet (MIT).
- 75 percent efficiency at 2-3 feet (Intel).





# Energy Harvesting and Energy Cooperation (EH-EC)

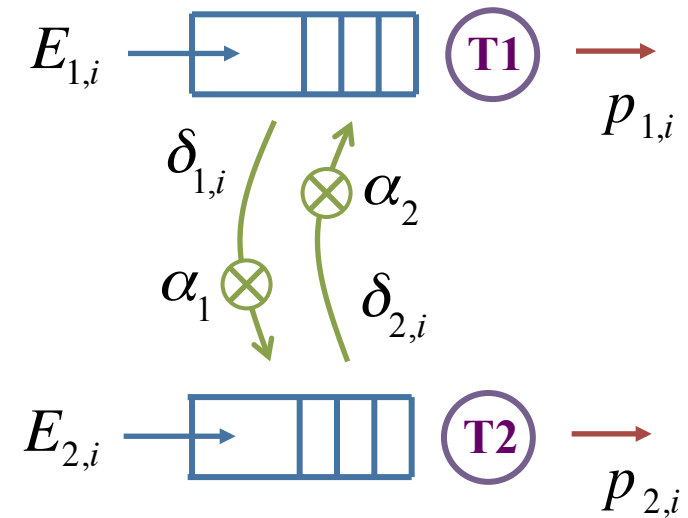
- $K$  transmitters receive energy  $E_{j,i}$  at the  $i^{th}$  time slot
- In slot  $i$ , node  $k$  transmits with power  $p_{k,i}$
- Transmitters wirelessly transfer energy to each other





## EH-EC

- In time slot  $i$ ,  $T_k$  sends  $\delta_{k,i}$  to  $T_j$ ,  $k, j = 1, 2$ , with end-to-end efficiency  $\alpha_k$
- Uni-directional EC is a special case with  $\alpha_2 = 0$
- Battery state at time slot  $i$ :



$$E_{k,i}^{bat} = \min \left\{ E_k^{\max}, E_{k,i-1}^{bat} + E_{k,i} - \delta_{k,i} + \alpha_j \delta_{j,i} - p_{k,i} \right\}$$

Harvested energy

Received and  
sent energy

Energy used for  
transmission



## Energy Constraints:

- **Non-negativity:**  $p_{k,n} \geq 0, \delta_{k,n} \geq 0, k = 1, 2, n = 1, \dots, N$

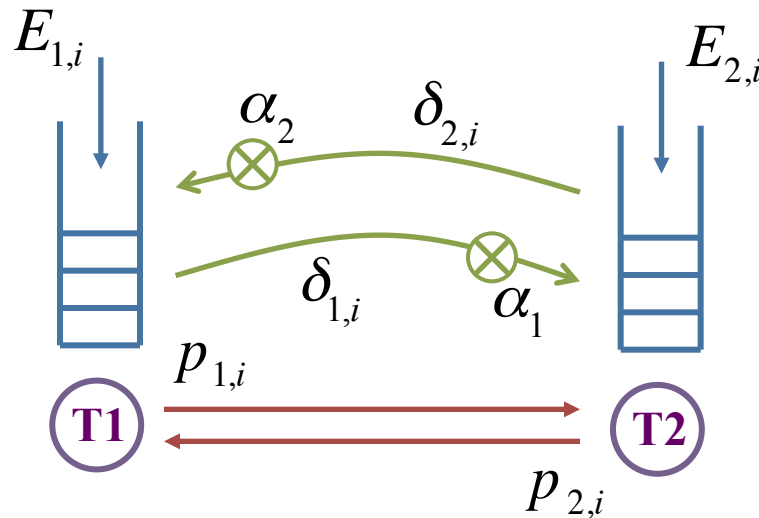
- **Energy causality:**  $E_{k,i}^{bat} = \sum_{n=1}^i (E_{k,n} + \alpha_j \delta_{j,n} - \delta_{k,n} - p_{k,n}) \geq 0$

- **No-Battery-Overflow:**  $E_{k,i}^{bat} \leq E_k^{\max}$





# EH-EC Two Way Channel



$$Y_1 = X_1 + \sqrt{h_2} X_2 + N_1$$

$$Y_2 = X_2 + \sqrt{h_1} X_1 + N_2$$

$$N_k \sim \mathcal{N}(0, \sigma_k^2),$$

- Sum-rate:**  $r^{TWC}(p_1, p_2) = \frac{1}{2} \log \left( 1 + \frac{h_1 p_1}{\sigma_2^2} \right) + \frac{1}{2} \log \left( 1 + \frac{h_2 p_2}{\sigma_1^2} \right)$



# Problem Statement

- Maximize sum-throughput by jointly optimizing the **transferred energy** and **transmit power**.

$$\begin{aligned} \max_{p_{k,i}, \delta_{k,i}} \quad & \sum_{n=1}^N r^{TWC}(p_{1,n}, p_{2,n}) \\ \text{s.t.} \quad & p_{k,i} \geq 0, \quad \delta_{k,i} \geq 0, \\ & \sum_{n=1}^i (E_{k,n} + \alpha_j \delta_{j,n} - \delta_{k,n} - p_{k,n}) \geq 0 \\ & j, k = 1, 2, \quad j \neq k, \quad i = 1, \dots, N \end{aligned}$$

- First assume infinite battery.



# Procrastinating Policies

- Definition: A **procrastinating policy** satisfies

$$p_{k,i} - \alpha_j \delta_{j,i} \geq 0, \quad k, j = 1, 2, \quad k \neq j$$

i.e., the energy received by a node is not greater than the energy required for transmission in each time slot.

- In a procrastinating policy, a node *does not transfer energy unless the receiving node intends to use it immediately.*
- Theorem: (Tutuncuoglu-Y.15): **There exists an optimal policy that is procrastinating.**



# Decomposition of the Sum-Throughput Problem

- Define **consumed powers**  $\bar{p}_{k,i} = p_{k,i} + \delta_{k,i} - \alpha_j \delta_{j,i}$
- Sum-throughput maximization can be **decomposed** as

$$\begin{aligned} \max_{\{\bar{p}_{k,i}\}} \quad & \sum_{i=1}^N r_S(\bar{p}_{1,i}, \bar{p}_{2,i}) \\ \text{s.t.} \quad & \sum_{n=1}^i (E_{k,n} - \bar{p}_{k,n}) \geq 0, \quad k=1,2, \quad i=1,\dots,N, \\ & \bar{p}_{k,i} \geq 0, \quad k=1,2, \quad i=1,\dots,N. \end{aligned}$$

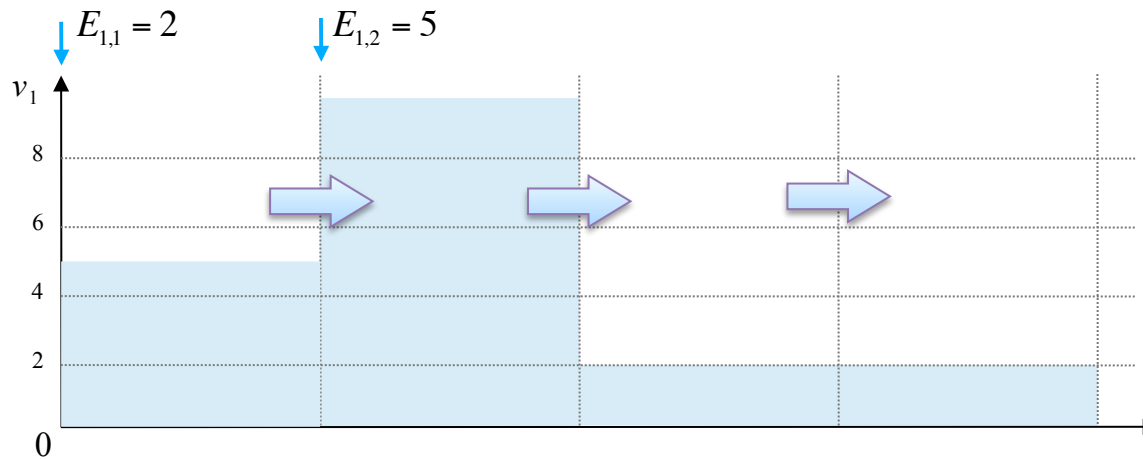
Power Allocation  
Solved via IGDWF

$$\begin{aligned} r_S = \max_{\delta_{k,i}} \quad & r^{TWC} \left( [\bar{p}_{k,i} + \alpha_j \delta_{j,i} - \delta_{k,i}] \right) \\ \text{s.t.} \quad & \delta_{k,i} \geq 0, \quad \bar{p}_{k,i} - \delta_{k,i} \geq 0, \\ & k=1,2. \end{aligned}$$

Energy Transfer  
Solved directly (single slot)

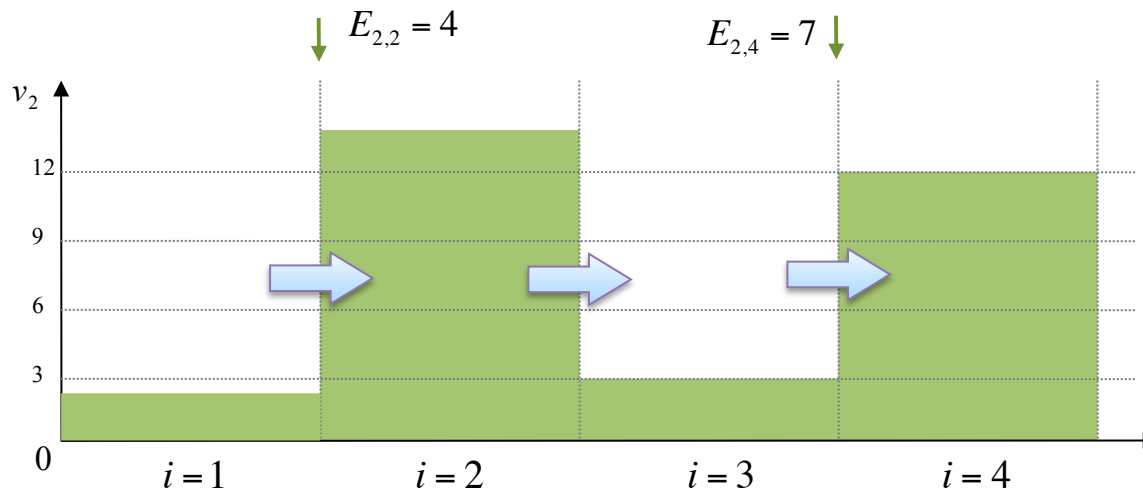


# EC-EH-TWC



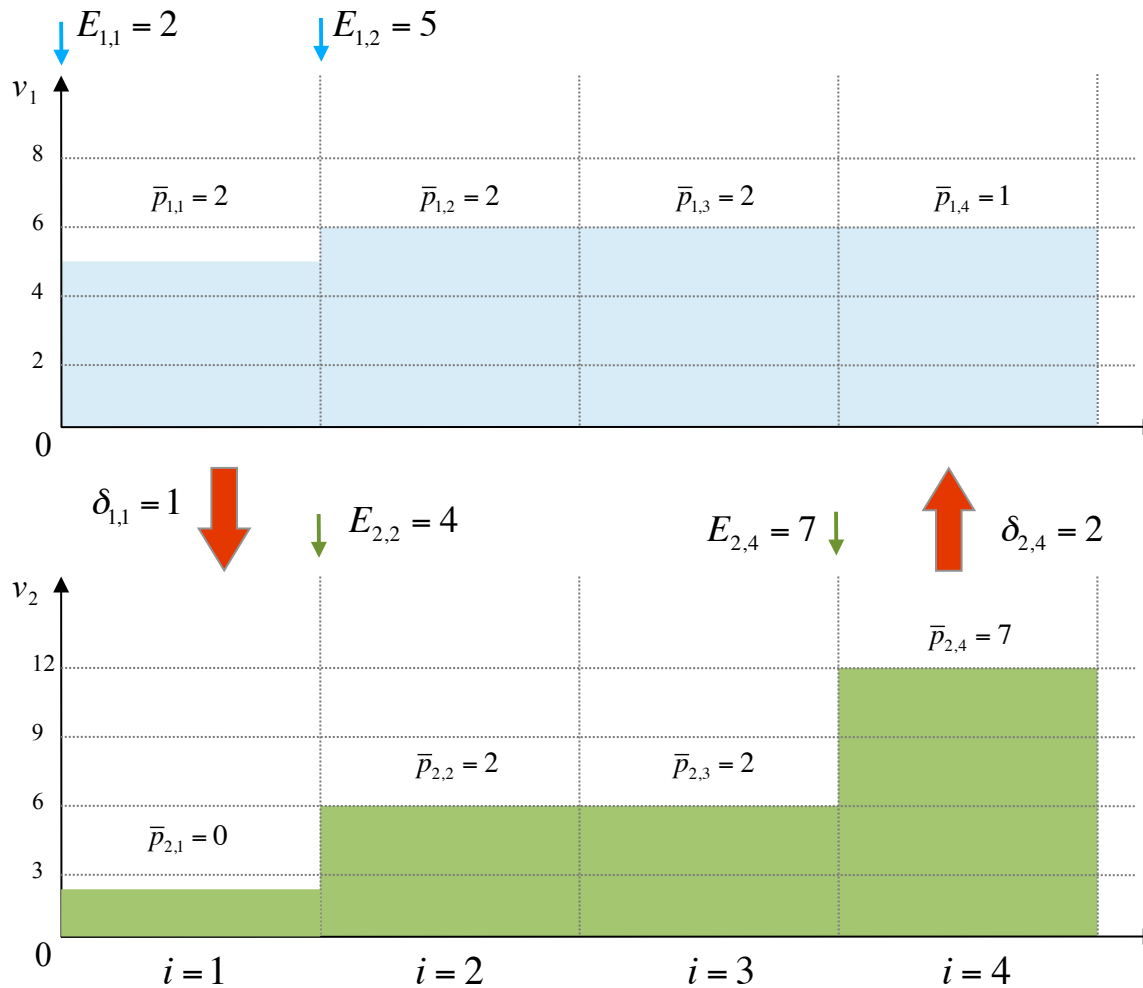
$$\alpha_1 = 0.5$$

$$\alpha_2 = 0.5$$





# EC-EH-TWC



$$\alpha_1 = 0.5$$
$$\alpha_2 = 0.5$$



# Finite Battery Extension [Tutuncuoglu-Y.15]

- Problem definition:

$$\begin{aligned} \max_{p_{k,i}, \delta_{k,i}} \quad & \sum_{n=1}^N r^{TWC}(p_{1,n}, p_{2,n}) \\ \text{s.t.} \quad & p_{k,i} \geq 0, \quad \delta_{k,i} \geq 0, \\ & 0 \leq \sum_{n=1}^i (E_{k,n} + \alpha_j \delta_{j,n} - \delta_{k,n} - p_{k,n}) \leq E_{k,\max} \\ & j, k = 1, 2, \quad j \neq k, \quad i = 1, \dots, N \end{aligned}$$

- Postponing energy transfers may result in **battery overflow**
- **Pure procrastinating policies no longer optimal**



# Partially Procrastinating Policies

- Split transferred energy as  $\delta_{k,i} = \gamma_{k,i} + \rho_{k,i}$ ,  $\gamma_{k,i}, \rho_{k,i} \geq 0$ .

←  
Immediately consumed comp.

→  
Stored comp.

- Definition:** A **partially procrastinating policy** satisfies

$$\begin{aligned} p_{k,i} - \alpha_j \gamma_{j,i} &\geq 0, & \gamma_{k,i} \gamma_{j,i} &= 0, & k, j &= 1, 2, & k \neq j \\ \rho_{k,i} (E_k^{\max} - S_{k,i}) &= 0, & & & k &= 1, 2, \end{aligned}$$

- Consumed comp. **must immediately be used**,
- Stored comp. **must be zero unless battery is full**.

- Problem solved via **2D directional water-filling with restricted transfers**





# Numerical Results

## ■ TWC:

$$N = 100, \quad T = 1\text{sec},$$

$$h_1 = -100\text{dB},$$

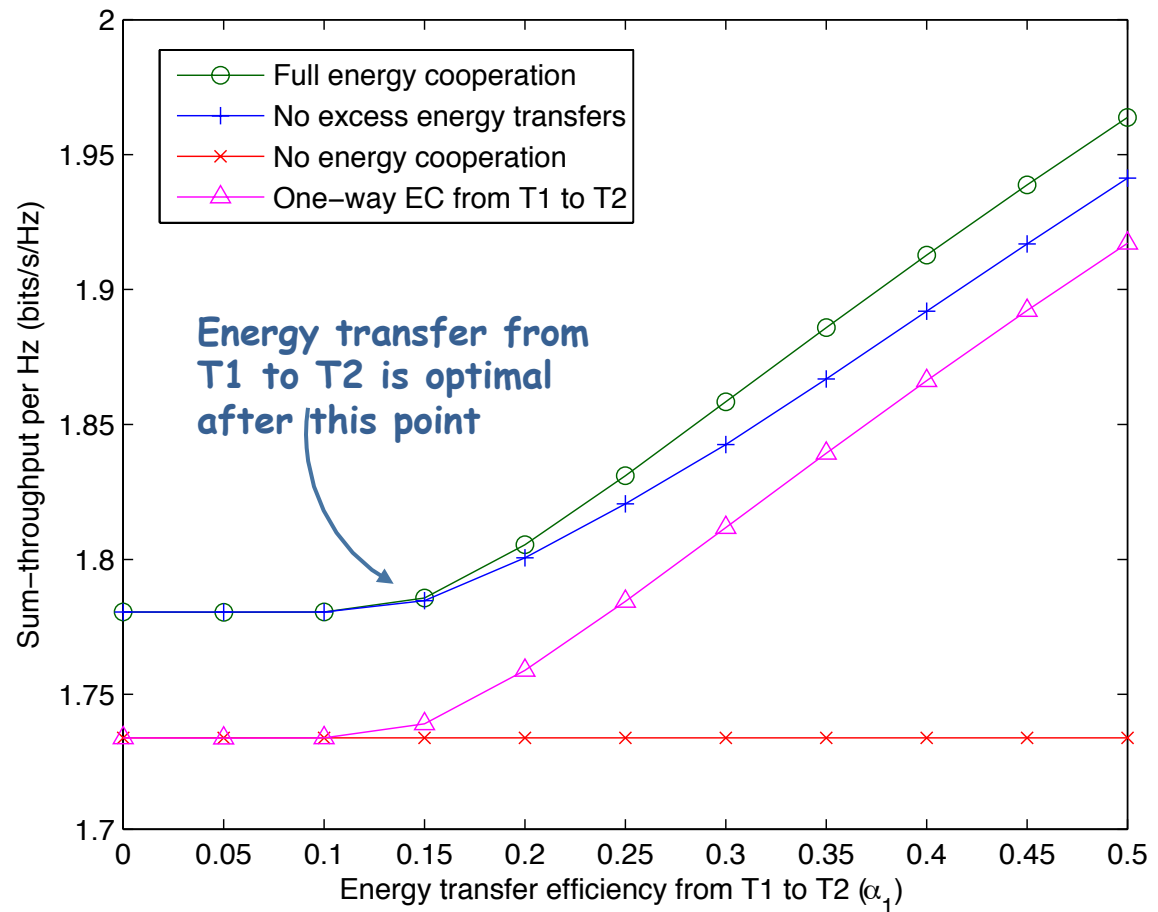
$$h_2 = -100\text{dB},$$

$$N_0 = 10^{-19} \text{ W / Hz}$$

$$E_{1,i} \sim U[0,10] \text{ mJ},$$

$$E_{2,i} \sim U[0,10] \text{ mJ},$$

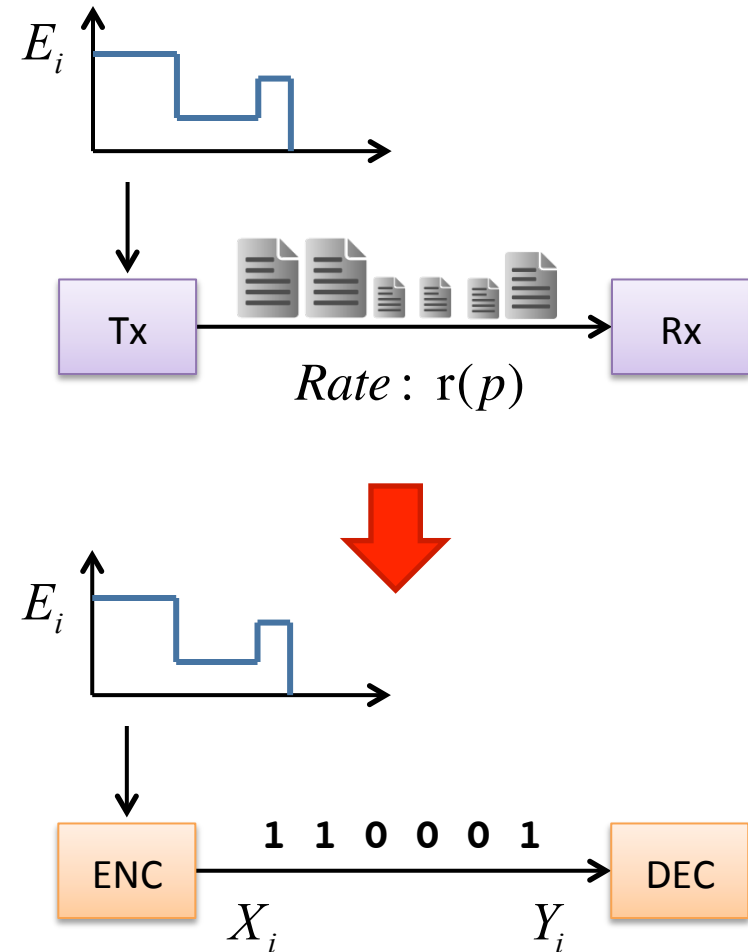
$$\alpha_2 = 0.5$$





# Information Theory of EH Transmitters

- So far, we have assumed **sufficiently long time slots** and utilized the known rate expressions.
- What if **energy harvesting is at the symbol level**, i.e., each input symbol is individually limited by EH constraints?

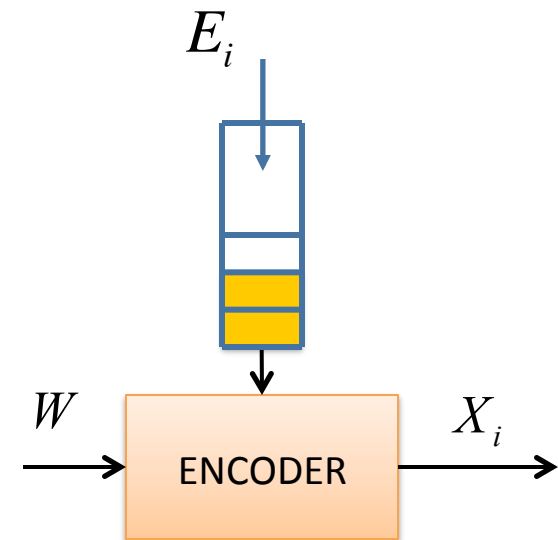




# Energy Harvesting (EH) Channel

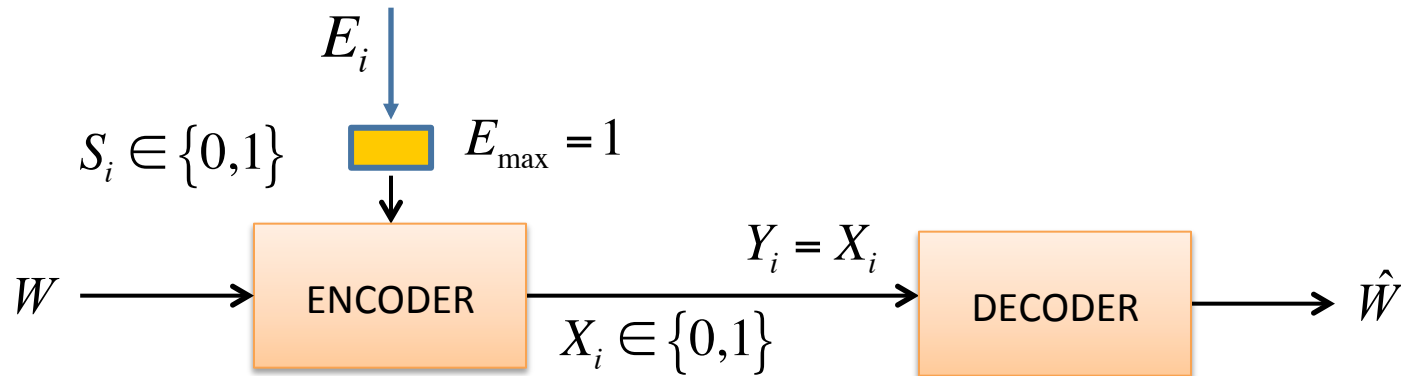
[Tutuncuoglu-Ozel-Ulukus-Y. '13]

- The **channel input** is restricted by an external **energy harvesting** process.
- **State**: available energy
  - Has **memory** (due to energy storage)
  - **Depends on channel input**
  - **Causally known to Tx (causal CSIT)**





# Binary Noiseless EH Channel



[Tutuncuoglu-Ozel-Y.-Ulukus '13, '14, 17']

- Transmitting  $X_i \in \{0,1\}$  requires  $X_i$  units of energy
- **Unit battery**,  $E_{\max} = 1$
- **Binary noiseless channel**,  $Y_i = X_i$



# Conclusion

- New wireless communications paradigm: **energy harvesting nodes**
- New design insights arising from
  - **new energy constraints**
  - **energy storage limitations and inefficiencies**
  - **interaction of multiple EH transmitters**
  - **energy cooperation**
- **New problems in the information theory domain**
- Still lots of open problems related to all layers of the network design.



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- Collaborators on papers summarized in this talk are: Omur Ozel, Kaya Tutuncuoglu, Sennur Ulukus, Jing Yang.



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